

# Theme V: Tall slender structures

Objekttyp: **Group**

Zeitschrift: **IABSE congress report = Rapport du congrès AIPC = IVBH  
Kongressbericht**

Band (Jahr): **9 (1972)**

PDF erstellt am: **25.05.2024**

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**V**

**Bâtiments hauts élancés  
Hohe schlanke Bauwerke  
Tall Slender Structures**

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## V

### DISCUSSION PRÉPARÉE • VORBEREITETE DISKUSSION • PREPARED DISCUSSION

#### **Westcoast Building Cable Suspended Structure Vancouver, B.C.**

Westcoast Building — Structure à câbles suspendus à Vancouver, B.C.

Westcoast Building — Seilverspannter Bau in Vancouver, B.C.

#### **B.B. BABICKI**

M. Sc., P. Eng., Principal of Bogue Babicki & Associates  
Consulting Engineers  
Vancouver, B.C. Canada

The Westcoast Office Building is located in Vancouver Canada in a very picturesque setting and on one of the major arteries of the city connecting the down town business core to the residential areas. This building has a total of 152,000 square feet of office area and covered parking accommodations for 200 cars. (fig. #1) It was designed for Westcoast Transmission Co. by Bogue Babicki & Associates, Consulting Engineers of Vancouver and construction completed in 1970.

Governing factors in the concept of the building were, the least interference with the natural setting and earthquake resistance since Vancouver is located on one of the severest earthquake zones extending from California to Alaska.

The building in its final form has a 277 foot high concrete centre core 36 x 36 feet in plan area and accommodating 21 levels from foundation to top as follows: (fig. #2)

Three underground parking levels, equivalent of three levels of open plaza space, twelve levels of typical office floors, 110 x 110 feet in plan area suspended from the centre core above the plaza space plus, three levels within the core above the roof for mechanical and elevator equipment.

This solution has the following advantages:  
The open plaza space under the building eliminates obstruction of a fine view of sea & mountains from the street level and isolates the first office floor from the direct effect of the street noise. Elimination of columns improves the efficiency of the underground parking. But, from a purely structural point of view as our main



concern, this system indicates a more favourable behaviour under seismic forces.

The reasoning behind this statement can be outlined as follows:

In most of the conventional high-rise buildings the vertical cores are used as main elements to transfer lateral forces but their contribution in supporting the vertical loads are very limited since the columns are made to carry most of the vertical loads. This arrangement results in an unfavourable stability and stress distribution in the core. By using the centre core to support all the vertical loads, the stability of the core is improved in transferring the lateral forces and the prestressing effect achieved due to the vertical loading, results in a more favourable stress distribution to the extent of eliminating tensile stresses in the core. In the case of this particular building these advantages were achieved within the dimensions of the core established for a conventional building.

Furthermore, a building supported on a single centre core element during an earthquake will behave in a more predictable manner for which it can be more realistically designed than the dynamically complex conventional buildings.

Due to the nature of this building and the prestressing effect on the core mentioned earlier it becomes obvious that the core is less susceptible to the damaging effect of the earthquake forces than the core of a conventional building and since the core carries all of the seismic loads, then the whole building is less susceptible to damage.

Once the rationality of the approach of carrying the full load on a centre core is established, a system for hanging the floors from the centre core was devised by the use of bridge strand continuous cables supported directly on the rounded top of the centre core and splayed to the outside perimeter of the building at the roof level. (fig. #3)

The use of cables continuous over the core eliminated the problem of splicing and anchoring of these hangers to the centre core

Six sets of  $2 \frac{3}{4}$ "  $\phi$  continuous cables are supported on a

centre core crown structure consisting of exterior core walls rounded at the top and two diagonal concrete arches. (fig. #4) The main roof beams which are provided with bearing saddles accommodate the change of direction of the continuous cables and transfer compression forces to a ring on the centre core. These beams are suspended by additional sets of cables which are draped over the core in a similar manner to the continuous cables.

The floor beams are simply supported at the core in pockets cast into the core walls, and are attached to the cables by means of friction clamps. (fig. #5) The floor system consists of a steel deck filled with concrete topping and attached to the beams with shear lugs to achieve composite action.

The centre core is treated as a free standing cantilever and supported on a 55 x 55 feet concrete raft foundation six feet thick. A 14 x 14 feet cut-out is provided in the centre of the foundation raft to distribute more evenly the stresses imposed on soil, thus minimizing the rocking of the building due to reversal of the lateral earthquake and wind loads.

This structural system with a definite delineation between the reinforced concrete and structural-steel parts, lends itself to a slip-form method of pouring the centre core. The concrete pour was a continuous twenty day and night operation, with an average speed of forms of 6-9 inches per hour.

The second stage of the construction was the erection of the roof girders and the draping of the floor-supporting cables. (fig. #6)

After completion of the draping of cables, the erection of the typical floors progressed at a rate of about one floor per day. (fig. #7) The 550 tons of G40.12 structural steel used averaged to a relatively light weight of only 7.5 lbs. of steel per square foot, and compares favourably with conventional construction.

Once the structural-steel erection was completed, the exterior curtain walls consisting of small aluminum mullions attached to independent light frames were connected to the floors only at the cable points. Solar bronze windows give a mirror-like appearance to the exterior skin. (fig. #8)

### Design Analysis:

We will concern ourselves with only two major aspects of the design analysis in the scope of this paper:

1. The design considerations of the concrete centre core.
2. Dynamic behaviour of the suspended system.

In designing the concrete core it was assumed to be a free standing cantilever fully fixed to the raft foundation. Horizontal roller type joints were provided on the parking decks where they met the core, to prevent the lateral support of the core by these decks.

In one direction the core walls contain no openings and for loads in that direction the core can be considered as a single cantilever thirty six feet deep with some flanges. In the other direction the multitude of openings tends to create two vertical elements instead of one. For example if the lintels from floors one to twelve have no stiffness, then the core would consist of two vertical elements in this region constrained to have the same horizontal deflection at each floor. These vertical elements would have the axial and bending of frame action. If on the other hand, the lintels had infinite stiffness one could assume a linear distribution of bending stress across the full thirty six foot depth. The real structure must be somewhere in between. The stress distribution is further complicated by the large opening at plaza level, numerous openings for ventilation ducts, and the solid upper part which adds stiffness to the system.

In order to determine this stress distribution, a finite element analysis of the core was run on a Univac 1108 computer by Hooley Engineering of Vancouver. Figure 9a shows how the core was modeled with 753 nodes, ~~666~~ rectangular finite elements in plane stress, and 389 pin ended members under axial load. At two degrees of freedom per node, this mesh generates a structure stiffness matrix with 1488 unknowns and a half band width of 22. Computer time comprised of a 2 1/2 min run. Data was generated within the computer with the openings represented by finite elements with zero modulus.

A more complex three dimensional analysis was not deemed necessary for this structure as the effect of walls at right angles could be easily included by the addition of vertical pin ended members. Five vertical lines, each consisting of an average of 80 of these two noded members, ran up the building to interconnect all vertical degrees of freedom on the line. Their areas duplicated the areas of the walls at right angles which they replaced except near the top where shear lag dictated a reduced area.

As mentioned previously, the stiffness of the lintel is all important in determining the stress distribution. For this reason a fine mesh of 54 finite elements was used to model a single lintel, as shown in Figure 9b. Horizontal pin ended bars represented the effect of the floor slab as top flange of the lintel. Such a mesh gave an excellent evaluation of stiffness for the lintel including shear deflection and the effect of the pocket for floor beams. The equivalent thickness of the two elements used on the full core to replace the lintel was chosen to duplicate the results of the fine mesh.

Stress at the element centre line was found from the stress matrix and eight nodal deflections. Summations of these shear and normal stresses over the thirty six foot width at several cross section together with the force in the bars, confirmed overall equilibrium to within one percent as a final check.

The very low slenderness ratio of the core shows no need to consider the moment induced by the action of vertical loads on horizontal deflections. A linear programme was then used and output confirmed this fact. As well, tilting of the foundation of this type of structure will not induce extra stress in the superstructure as would be the case if a frame surrounded the core.

The above analysis was carried out for the three load vectors corresponding to dead and live load, wind, and earthquake. Since the magnitude and distribution of seismic loads depends upon the natural frequency and shape of the first few normal translational modes, it was necessary to calculate these first. Rather than find frequencies from the full structure matrix of order 1488 a

reduced structure matrix was generated of order ten. This is best done by the application of ten loads, one at a time, to ten points equally spaced (approximately) up the core. The ten deflections at these ten levels then give one column of the reduced flexibility matrix. A standard eigenvalue subroutine together with ten masses gave the first three mode shapes and frequencies with sufficient accuracy.

In the dynamic behaviour of the suspended system a major concern was the close proximity of the natural frequency of the centre core with the natural frequency of the suspended system.

To improve on the dynamic behaviour of the structure as a whole, it had to be considered that the translational mode of vibration of the core will have minimal effect on the vertical vibration of the suspended system. After the analysis and design of the suspended system for the vertical loads a dynamic analysis for the natural frequencies of this system was carried out and found to be well separated from the first and second modes of vibration of the centre core. (fig. #10)

The behaviour of this building during an earthquake was one of the considerations in the concept of this building. Our analysis of this building has revealed no adverse effect due to this system. In fact this building has a longer period than if it had a surrounding rigid frame and falls well below the peak acceleration of the classical earthquake spectrum of El Centro, consequently generates smaller seismic forces. (fig. #11)

For the very same earthquake consideration a research programme was devised and in two construction stages of this building various dynamic test using a vibration generator, were carried out.

Actual dynamic properties of this building were learned and the structure reanalysed under the light of this information. This research and its findings will be the subject of another paper in the near future.

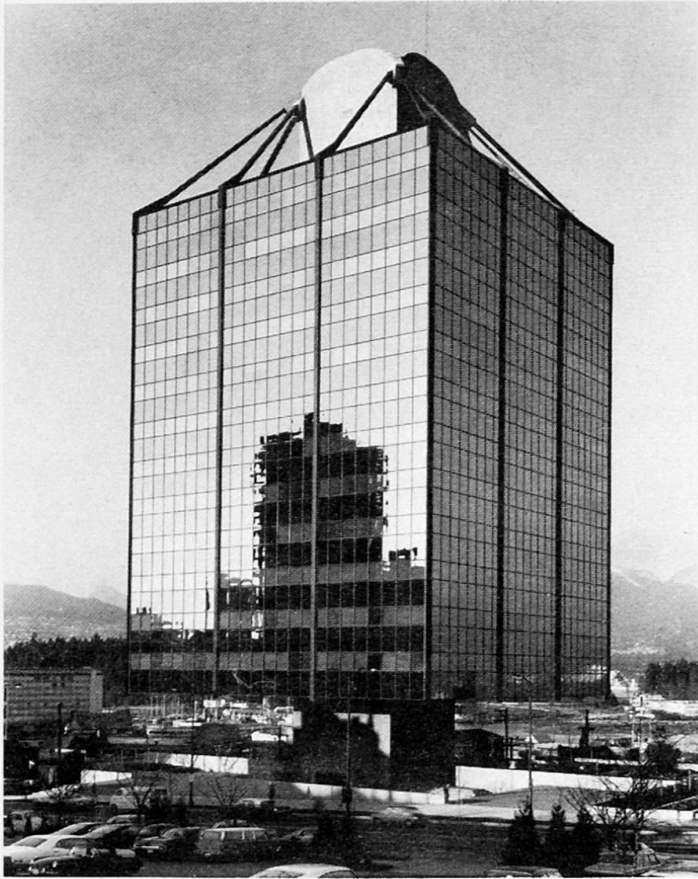


Fig. 1  
The Westcoast Office Building

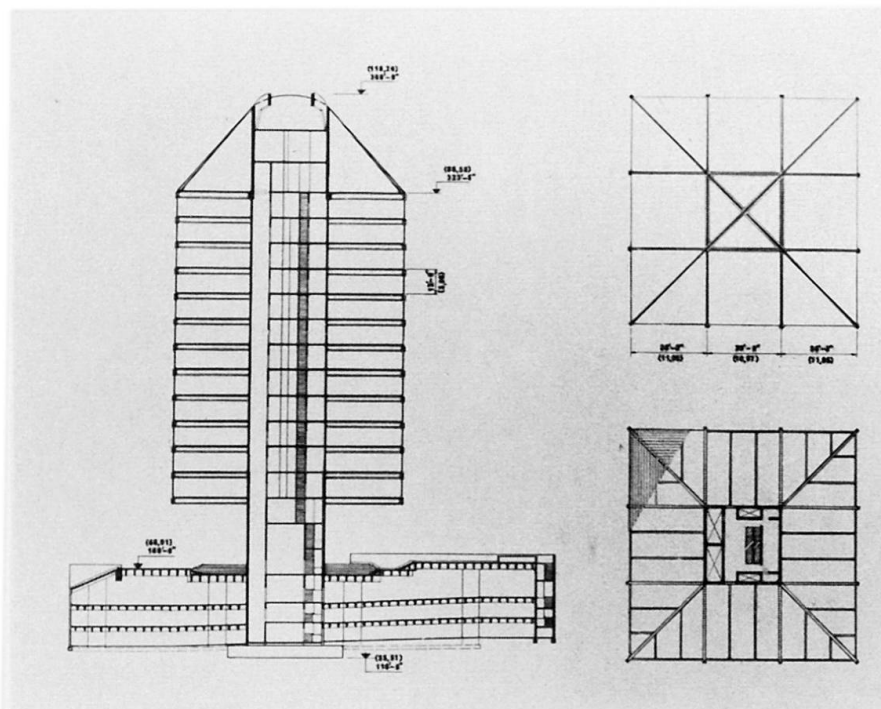


Fig. 2  
Building in its Final Form



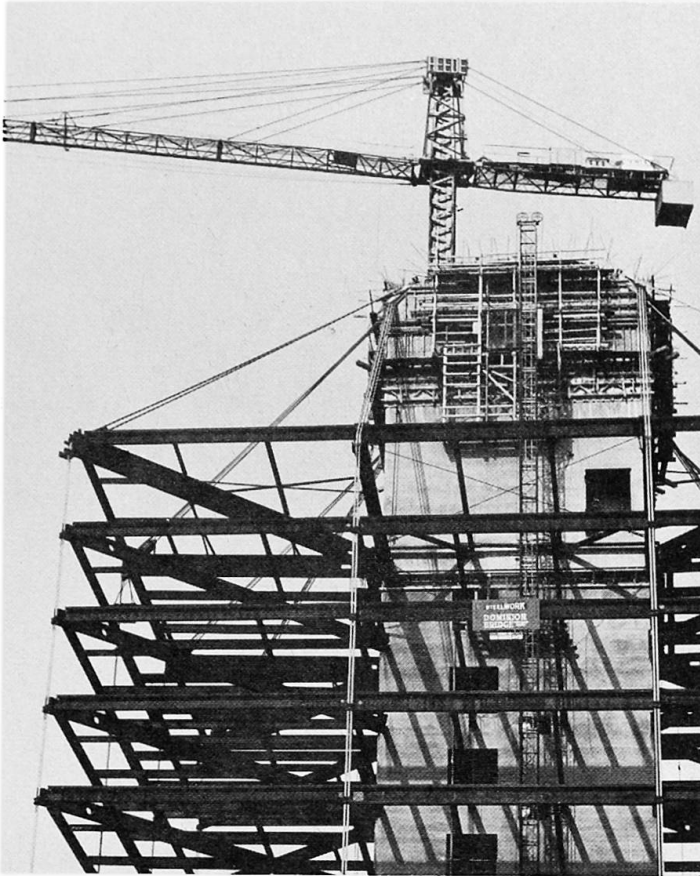


Fig. 3  
A System for Hanging the  
Floors from the Centre Core

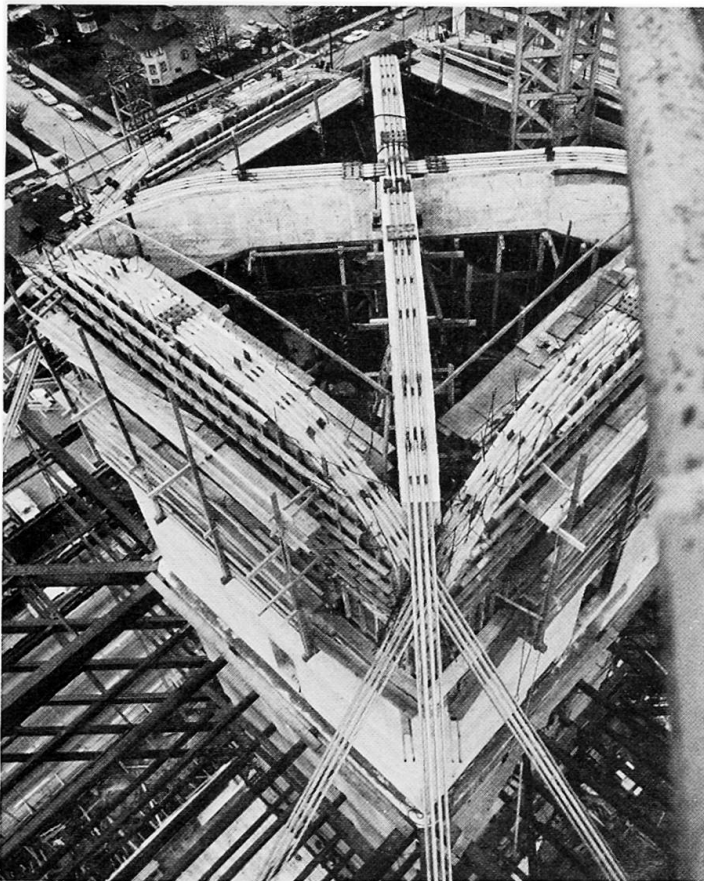


Fig. 4  
Six Sets of Continuous  
Cables Supported on a  
Centre Core

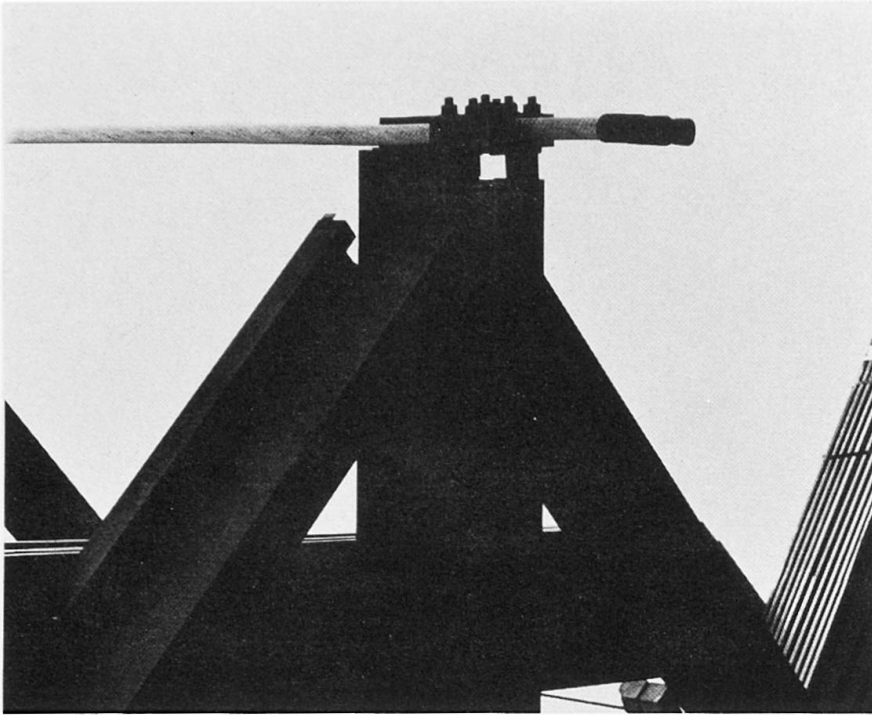


Fig. 5  
The Floor Beams Attached to  
the Cables by Means of  
Friction Clamps

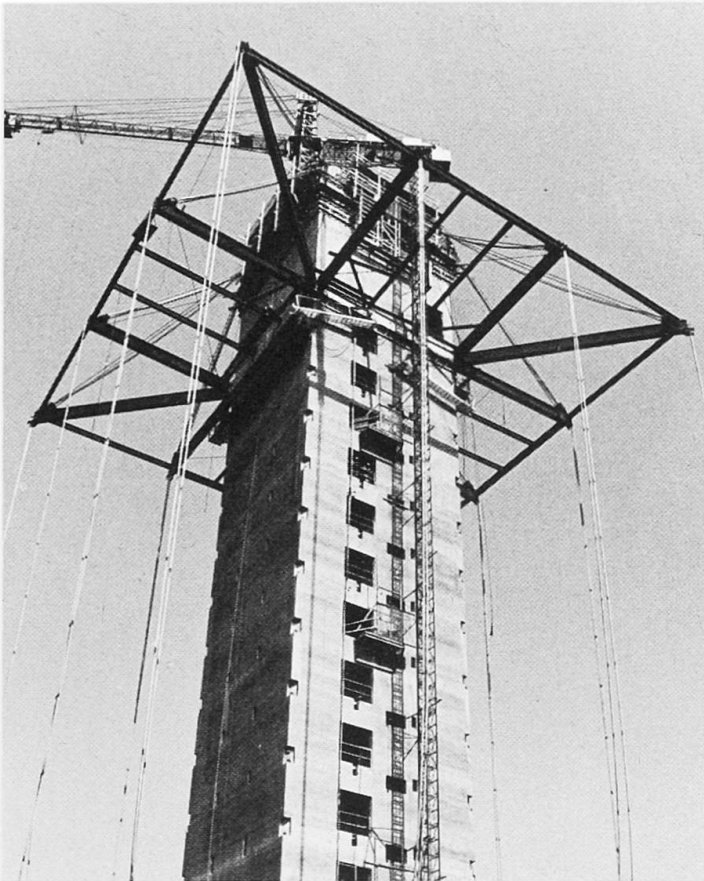


Fig. 6  
Second Stage of Construction  
Erection of Roof Girders and  
Draping of the Cables



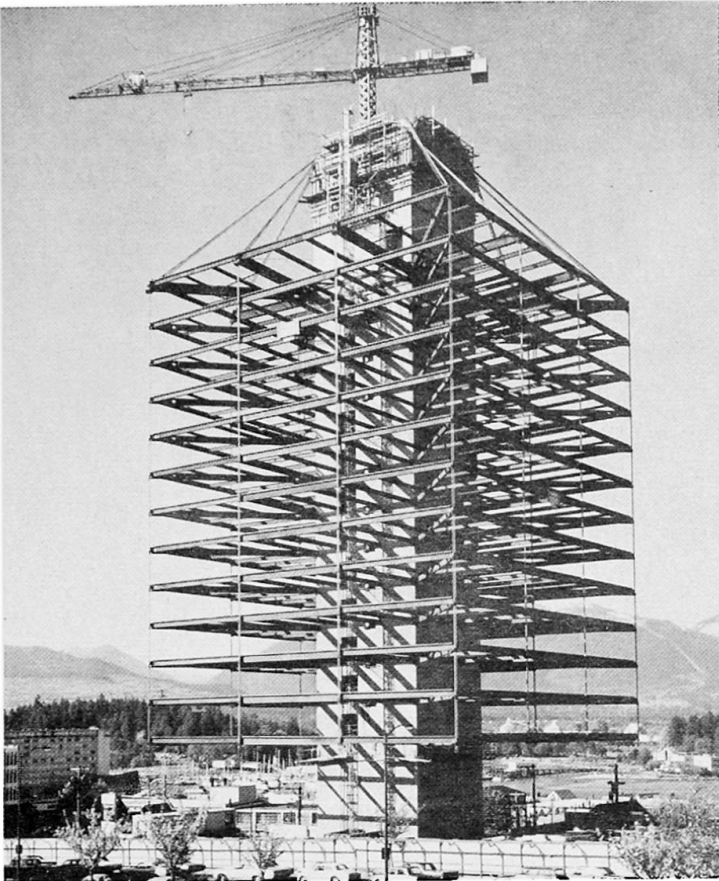


Fig. 7  
Erection of the Typical  
Floors Progressed at a Rate  
of about one Floor per Day

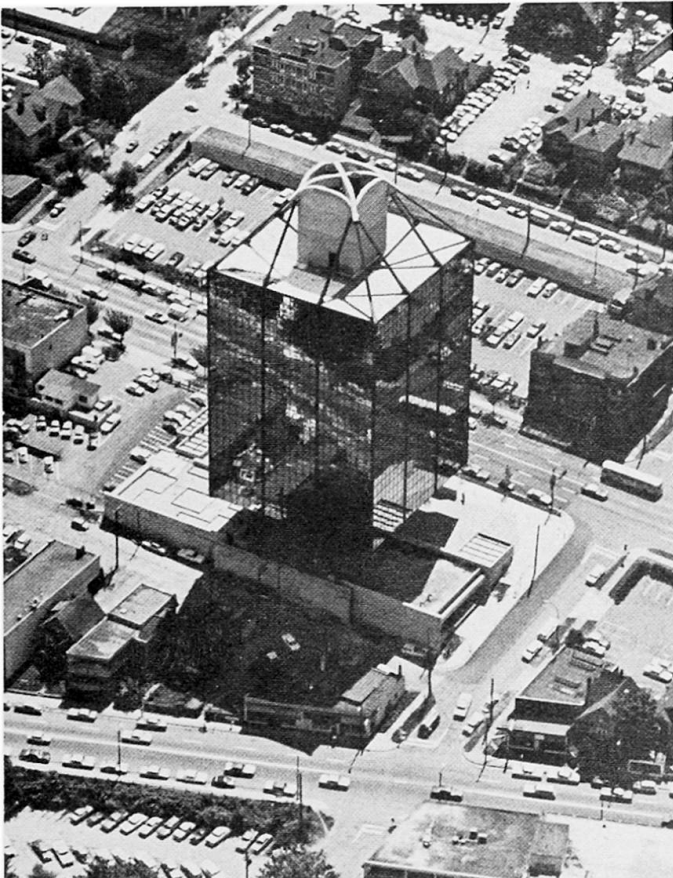
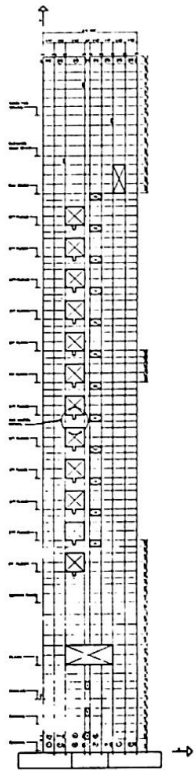
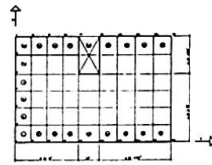


Fig. 8  
Mirror-like Appearance to  
the Exterior Skin

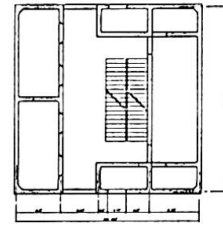
Fig. 9  
Network of Finite Elements



a) Core Elevation



b) Lintel Detail



c) Core Section

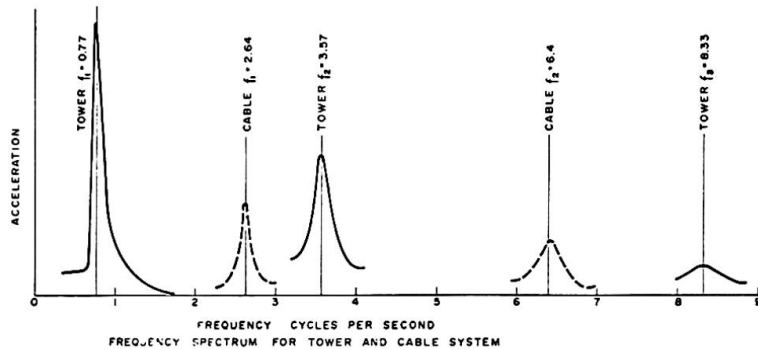


Fig. 10

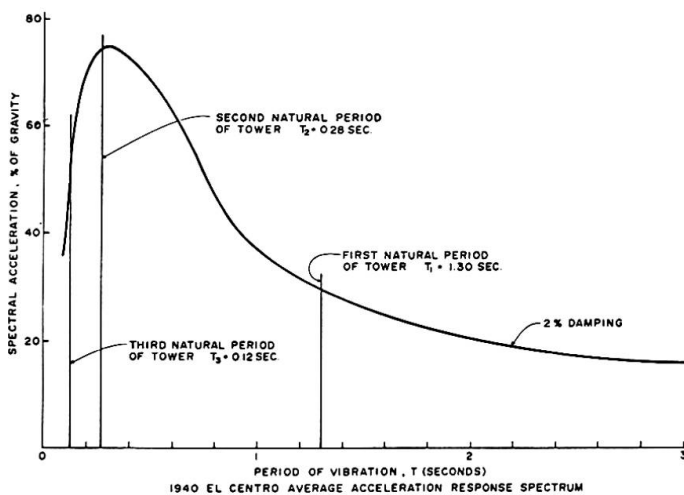


Fig. 11

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## **Alternative Analysis of Stress and Frequency of a Structure of the Type of West Coast Transmission Building in Vancouver, B.C. Canada**

Analyse alternative des tensions et des fréquences d'un immeuble du type "West Coast Transmission Building" à Vancouver, B.C. Canada

Alternativberechnung der Spannungen und Schwingungen eines Gebäudes vom Typ "West Coast Transmission Building" in Vancouver, B.C. Kanada

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### General

The recently constructed West Coast Transmission Office building in Vancouver is very original in design (Fig.1). It was designed and analyzed by B. Babicki and Associates, Consulting Structural Engineers. The authors were not connected in any way with the design and analysis of that building, and this paper presents an alternative method of analysis to the one actually used, of which the authors have no particulars. Its thirteen main floors, 108' x 108' in plan hang by cables on the central reinforced concrete core 36' x 36' x 265' high. This type of support improves greatly the behaviour of the structure in an earthquake, and the prestressing effect of the weight of the building makes the core much stronger in resistance to lateral loads. Furthermore, the absence of columns provides maximum usable space in the floor areas.

The floors are made of reinforced concrete slab extending over steel beams, whose inner ends rest in the core wall recesses, and the outer ends are attached to the cables, hanging vertically on the outside of the building. Above the upper floor the cables are sloped and draped over the core. With this arrangement part of the weight of the floors is carried by the beams directly to the core and the rest is applied by cables at the top of the core. The floor areas inside the core are used for elevators, stairs and services, requiring numerous large openings in the walls.

Although the distribution of load between the core and the cables is statically determinate, the stress analysis of the core is somewhat uncertain. The conventional beam formula is inapplicable in view of the presence of openings, and its approximate adaptations are unsuitable because the openings are irregular. The authors feel that their treatment of the problem by the method of finite element, although not fully rigorous, is most appropriate.

### The Finite Element Model of the Core and the Loads

In a structure of high complexity the use of simplifying assumptions is unavoidable. The core is definitely unsymmetrical about the central plane XZ (or North-South), and is treated as

such, but its minor asymmetry about the plane YZ (or E-W) is disregarded. Since the core walls are comparatively thin (14" and 10"), their flexural rigidity is ignored, and they are treated as in a state of plane stress.

The finite element model of the half of the structure on one side of the plane of symmetry (Fig.2) consists of as many as 726 rectangular two-dimensional finite elements or no-bar cells of 172 different sizes filling the exterior and most of the interior (not shown in Fig.2) walls. That so many cells are required in the model is determined by the need to match the wall openings. Two tiers of elements are as a rule required for the height of each storey. Some of the interior walls, judged non-contributory to the stiffness of structure are omitted from the model, and so are the interior stairs and the floors within the core. The elastic properties of the model are taken: the modulus of elasticity  $E = 3,000 \text{ kips/in}^2$  and the Poisson's ratio  $\mu = 0.2$ . The contribution of reinforcement to the stiffness of the structure is not considered.

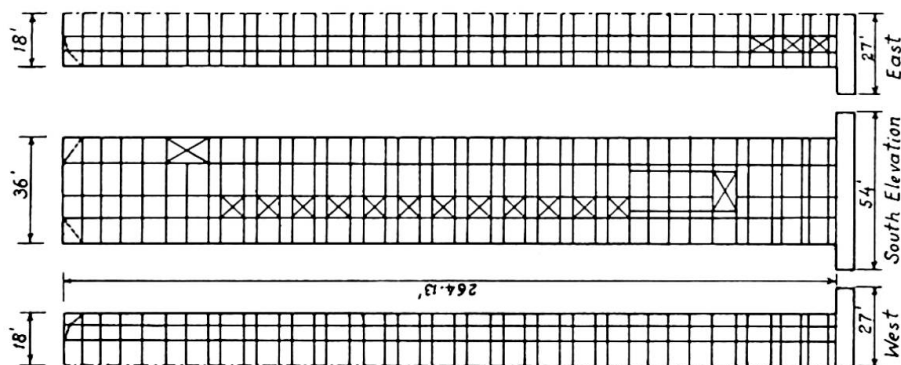


Fig. 2

The loads used in the analysis are: dead load, live load on all floors of one half of the maximum intensity, or in lieu of it, of full intensity on one half of the whole building, and the horizontal static loads, purported to imitate the actions of wind and earthquake. The intensities of all these were established by the designer in accordance with specifications.

The additional effects on stresses of the lateral deflection of the structure and of tilting of its foundation are also provided for. Although of minor importance in this particular structure, they may be very significant in more slender buildings.

By way of simplification all loads at their respective levels are applied at the core corners. The error resulting from this partial misplacement of loads is purely local, and it vanishes quickly on the way down. All nodes not common to two intersecting walls are restrained from moving out of the plane of the wall to which they belong. In the actual structure this restraining action is provided by the floors and the flexural rigidity of the walls, both of which are left out in the model.

#### Outline of Analysis.

The computer combines the matrices of individual cells into the stiffness matrix of the model and solves the numerous simultaneous equations for the displacements of the nodes. Products of the cell stiffness matrices and their displacement vectors give the load vectors of cells, from which are found the normal and tangential force concentrations at all nodes in several more highly stressed horizontal sections. By spreading these over the tributary areas of the adjacent cells stresses in the prototype are deter-

mined, - this is known as the method of nodal force concentrations. The other method for finding stresses, making use of nodal displacements, is mostly suitable for models composed of regularly spaced cells of one kind, uninterrupted by openings and irregularities. It was not used in this case.

Stress analysis outlined here is based on undeformed structure. Actually however, there is some lateral deflection bringing with it additional flexural effects, and a special procedure is devised to provide for them.

From the study of soil conditions an estimate is made of the amount of tilting of foundation by the action of horizontal forces and the one-sided live load, both assumed to act in easterly direction, more unfavorable than northerly. Tilted base makes the axis of the core inclined, which results in creation of bending moments by the dead and live loads all along the core. These flexural effects are augmented by the core's horizontal deflection. The amount of this deflection is unknown at the start, but the shape of the deflected axis may be closely approximated by any reasonable curve, such as a quadratic parabola. The amount of deflection at the top is assumed, and the deviation of the axis, and with it the resulting bending moments all along the axis are determined. The flexural deflection produced by them is now found by computer and compared with the assumed. If they disagree, the procedure is repeated with a new estimate of deflection. The assumed tilting of foundation may also be revised in response to the changed base moment.

### Stresses by Nodal Force Concentrations.

The horizontal sections chosen for stress determination are the ones whose stresses are likely to be high, as on the lines of openings, especially where the wall thickness changes from 14" to 10". The procedure for converting the nodal force concentrations in the model into the stresses of the structure itself is more complicated here than in plates under plane stress, because of the walls meeting at an angle and the presence of openings. The method is illustrated on the example of junction K of three cells 1, 2 and 3, whose arrangement and dimensions are shown in Fig. 3. Three

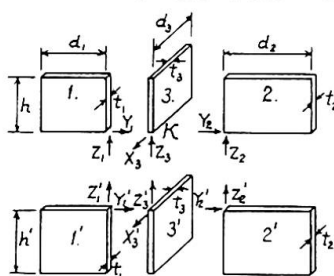


Fig. 3

similarly arranged cells 1', 2' and 3' are present underneath. For simplicity they are assumed of the same thicknesses as the ones above. The equality of vertical strains in the walls at the node K, combined with the low stress level in the horizontal direction and the smallness of Poisson's ratio, allow to assume that the vertical normal stresses in all walls are equal. With further assumption, that the contributions of the nodal concentrations Z to the normal stress decrease linearly to nothing from K to the adjacent nodes, the normal stress on the horizontal plane at K is

$$\sigma_z = \frac{2(Z_1 + Z_2 + Z_3)}{t_1 d_1 + t_2 d_2 + t_3 d_3} \quad (1)$$



The part of the component  $Z_1$  contributing to this normal stress is  $\frac{t_1 d_1 (Z_1 + Z_2 + Z_3)}{t_1 d_1 + t_2 d_2 + t_3 d_3}$ . Therefore, the balance of it

$$V_{Z1} = Z_1 - \frac{t_1 d_1 (Z_1 + Z_2 + Z_3)}{t_1 d_1 + t_2 d_2 + t_3 d_3} \quad (2)$$

contributes to the vertical shearing stress. Similar nodal force  $V_{Z1}'$  (upward) is found in the cell 1' below the cell 1, and so the the vertical shearing stress in the structure to the left of the

$$\text{point K is } \tau_{yz} = \frac{2(V_{Z1} + V_{Z1}')}{t_1 (h + h')} \quad (3)$$

With no Y concentrations in the cells 3 and 3' the normal stress on the plane Y to the right of the point K is

$$\sigma_y = \frac{2(Y_2 + Y_2')}{t_2 (h + h')} \quad (4)$$

The shearing concentration between the cells 2 and 2' is

$$V_{zy} = \left[ Y_2' - \frac{h' (Y_2 + Y_2')}{(h + h')} \right] \quad (5)$$

$$\text{and the shear stress } \tau_{zy} = \frac{2V_{zy}}{t_2 d_2} \quad (6)$$

The shear stress  $\tau_{zy}$  on the left of the node K is numerically different from the one in Eqn.(6) in view of the presence of shear flow, coming from the interior wall of the cell 3, but it can be found by an equation similar to Eqn.(6). For the same reason the shear stresses  $\tau_{yz}$  in Eqn.(3) are also different on the right and left of K.

#### Stresses Near Openings.

The presence of openings leads to some difficulties. Consider an element A between any two of the lower openings in the core wall. In general each of the two perpendicular nodal components in a cell represents the sums of the effects of the normal stresses on one of its adjacent sides and of the shear stresses on the other. Since however the cell A has no adjacent neighbors above and below it, its vertical nodal components designated S in Fig.5 must be viewed as representing only the shear contributions from the vertical sides, and, for the same reason, the horizontal components N - the normal effects on the vertical sides.

Determination of stresses in the prototype structure by distributing the nodal forces in the cell A in a manner described earlier leads to the presence of shear stresses on the vertical sides of the area A, as in Fig.6, and their absence along the horizontal sides contrary to the basic principle of statics.

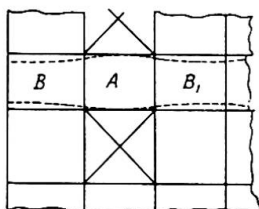


Fig. 4

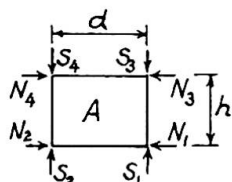


Fig. 5

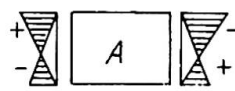


Fig. 6

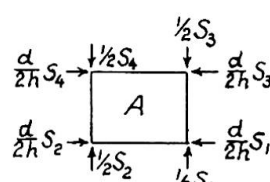


Fig. 7

It appears that the procedures devised for determination of stresses in the opening-free areas are not consistent with the stress - deformation conditions present around the openings. A qualitative examination of these conditions, illustrated on the example of the cell A and its neighbors in Fig.4 is useful. The part of the core on both sides of the opening becomes compressed and

shortened, while the area A remains largely uncompressed, except on the sides, as indicated by the dotted lines. The inclinations of these lines near the sides of the area A point to the presence of vertical shear stress in substantial agreement with Fig.5, and also to some edge compression in the area A, in contradiction to the earlier advanced significance of the nodal forces in the figure. It appears then that the nodal forces S should stand partly for the normal stress on the horizontal sides of the area, unprovided in the distribution procedure formulated earlier. Similarly, the nodal forces N should stand also for the shearing stresses on the horizontal edges of A. With no rigorous resolution for this dilemma, the authors' suggestion based on judgment is to attribute to shear actions the parts of the nodal forces shown in Fig.7, relegating their balances to the normal stresses.

It is necessary to point out that the stress irregularity caused by openings is not confined to their immediate vicinity, but is extended to the nodes one or even more steps away from them, where the computed shearing stresses on the horizontal and vertical planes are likely to come out unequal, and for this reason should be averaged up.

A considerable improvement of stress results may be effected by subdividing the cells one in four. A fine cell model of this kind of a complete structure may increase unreasonably the computer time, but it is quite appropriate to restrict this subdivision to a part of the structure under immediate investigation, attributing to its boundary nodes the displacements found in the coarse cell model.

#### Analysis and Design.

It is desirable to say a few words on the design of the structure, as distinct from the subject of this work, the stress analysis. The full extent of the high shearing stresses in the vicinity of openings created by the dead weight should be considered primarily as a warning, rather than the actual design condition. On the one hand it may be improved by reinforcement and prestressing and on the other be relieved automatically by creep in concrete as the stress builds up in the course of construction, while the material is comparatively fresh. The high shear stresses are also largely participation stresses, and not the load carrying stresses.

#### Vibration Frequency and Finite Element Model.

In the earthquake prone region like Vancouver the behavior of the structure under an earthquake is of primary importance. This is largely characterized by the magnitude of the lowest frequency of its vibration, which in case of the West Coast Transmission building corresponds to the flexural deflection of its core as a cantilever beam.

This vibration frequency is also determined by the method of finite element with employment of some additional assumptions. The structure is treated as symmetrical about both XZ and YZ planes, thus making the vibratory oscillation from the position of equilibrium fully antisymmetrical with reference to XZ plane.

The core is subdivided into one storey box-like elements consisting of floors and core walls (Fig.8). The massive foundation slab, resting on elastic underground forms the element #1 surmounted by the core elements 2 to 22. The last of these, trapezoidal



in shape, is replaced by a rectangular one for the sake of a substantial simplification of analysis. Vertical cable lengths within the storey heights and the sloping parts of cables at the top form additional units.

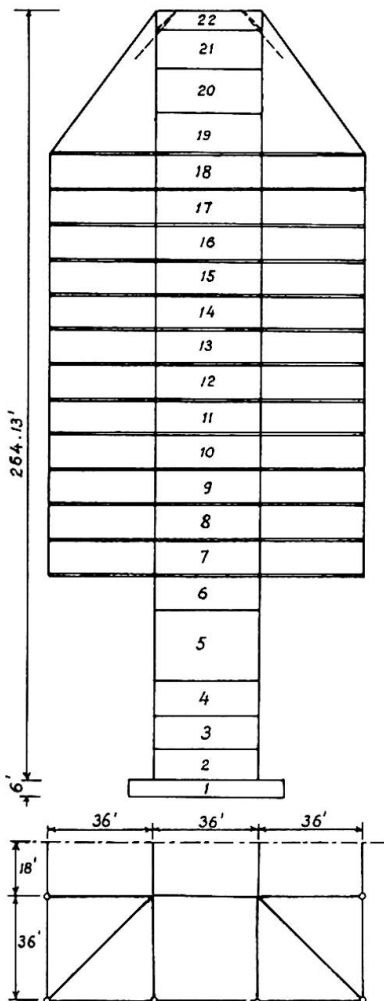


Fig. 8

a cell below is at the same time the bottom node of the cell above. The same applies to the top and bottom nodes of the three cable lengths in one storey within a quadrant of the structure. This makes the number of independent displacements of the structure

$$1 + 2(21) + 3(13) = 82.$$

#### Eigenvalue Equation. Stiffness and Mass Matrices.

Vibration of the structure is subject to the eigenvalue equation:

$$([K] - \omega^2[M])\{\delta\} = 0 \quad (7)$$

in which  $\{\delta\}$  is the 82 term vector of absolute displacements of the model,  $\omega$  is its angular frequency and  $[K]$  and  $[M]$  are the stiffness and the mass matrices of the model.

The terms of the matrix  $[M]$  are the masses of the parts of the core and the suspended floors tributary to each  $\delta$  and they are determined directly by apportioning between the nodes the masses of all parts, i.e. of the interior and exterior walls of the core and the floors both inside and outside of it.

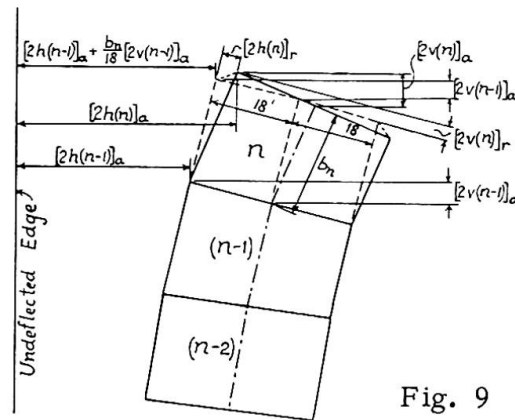


Fig. 9

In view of dual symmetry of the structure and antisymmetry of the vibratory motion, its displacements are fully described by the movements of nodes of a single quadrant. The rigidity of suspended floors in their planes makes their horizontal displacements equal with those of the core corners. On the other hand the concrete floor slabs are thin and flexible, while the floor beams carrying their loads to suspenders are very rigid. This permits to assume the vertical deflections of the cable nodes independent of similar deflections of the other cable nodes and the core corners in the same floor.

Motion of cell 1 is described by one node moving only vertically, while motions of the other core cells are described by two nodes moving in Y and Z directions. The top node of

The terms of the stiffness matrices of core cells are determined by the relative and not the absolute displacements of nodes. In each element for these are used the horizontal and vertical displacements of the upper corners in relation to the lower corners, thus forming  $4 \times 2$  stiffness matrices of core cells except the cell 2, having  $3 \times 2$  stiffness matrix, because its bottom node, sitting on the foundation cell, does not move horizontally. The matrix of the foundation cell possesses only one term. The contributions of the cable lengths to the stiffness matrix are determined by their cross-section areas and the relative movements of the ends.

To solve the eigenvalue equation the stiffness matrices of cells must be related to the absolute displacements, similarly to the mass matrices. Call the vertical and horizontal relative displacements of the upper node 2 relatively to the lower node 1 in the core cell  $n$  respectively  $[2v(n)]_r$  and  $[2h(n)]_r$ , and the absolute displacements of the same node  $[2v(n)]_a$  and  $[2h(n)]_a$ . Consider these quantities as infinitesimals of the first order and ignore the infinitesimals of the second order. This means that the vertical projection of the deflected axis of the core remains equal to its undeflected length, and the horizontal sides of the cells are no different in length from their horizontal projections after deflection. The following relations are then obtained by geometry (Fig.8):

$$\left. \begin{aligned} [2v(n)]_r &= [2v(n)]_a - [2v(n-1)]_a \\ \text{and } [2h(n)]_r &= [2h(n)]_a - [2h(n-1)]_a - \frac{b_n}{18} [2v(n-1)]_a \end{aligned} \right\} \quad (8)$$

In these equations  $(n-1)$  is the number of the cell below  $n$ ,  $b_n$  is the height of the cell  $n$  and 18 feet is its half-width.

The terms of the stiffness matrix  $[K]$  of the whole model in Eqn.(7) are found by combining the terms in the two adjacent elements with replacement of the relative nodal movements by their absolute equivalents in Eqns.(8). The eigenvalue equation is solved for its first frequency and mode vector by one of the standard procedures.

#### Check of the Method.

As a numerical check on the finite element method of frequency analysis employed here it was applied to a vertical fixed-ended cantilever beam of constant box section with dimensions and length comparable to the core of the structure under consideration, subdivided into a similar number of equal box-like cells without tops and bottoms. The finite element frequency was found close to the one determined by the standard formula of elasticity.

#### Conclusion

The authors consider it unnecessary to include here the numerical results of their calculations both for the stresses and the frequency of vibration, since present work represents an alternative method and not a part of the design and original analysis for which they were not responsible and were not in possession of all the necessary data. Thus the actual rigidity of the underground and its elastic response to vertical deformation were unknown to them and were simply assumed. The same applies to the elastic properties of the cables, known only by their diameters and not by the composition and sizes of strands and wires.

The authors admit some arbitrariness in the recommended procedure for determination of stresses near the openings, but they believe the finite element method proposed here is most suitable for analysis of structures of the type of West Coast Transmission building.

### Notation

a	subscript signifying "absolute"
b	height of cell number n.
d	with subscripts, - widths of cells.
h, v	parts of symbols, signifying horizontal and vertical.
h, h'	heights of cells.
t	with subscripts, - thicknesses of cells.
r	subscript signifying "relative"
E	modulus of elasticity.
[K]	stiffness matrix.
[M]	mass matrix.
N	with subscripts, - nodal components caused by normal effects.
S	with subscripts, - nodal components caused by shear effects.
V, V'	shearing parts of nodal force concentrations.
Y, Z	with subscripts, - nodal force concentrations.
XYZ	coordinate axes.
{ $\delta$ }	vibratory deflection vector.
$\mu$	Poisson's ratio.
$\sigma$	with subscripts, - normal stresses.
$\tau$	with subscripts, - shearing stresses.
$\omega$	angular frequency.

### References

1. A. Hrennikoff: Precision of Finite Element Method in Plane Stress; Proceedings, International Association for Bridge and Structural Engineering, Zurich, Switzerland, Vol. 29-II, 1969.
2. O.C. Zienkiewicz and Y.K. Cheung: The Finite Element Method in Structural and Continuum Mechanics. McGraw-Hill Publishing Co., London.
3. B.B. Babicki: Cables Support Office Building, Civil Engineering, October, 1971. ASCE, New York.

### SUMMARY

The thirteen main floors of this office building 108' x 108' in plan hang by cables on the central reinforced concrete core 36' x 36' x 265' high. The small area of the foundation and the prestressing effect of loads make this structure highly resistant to earthquakes and flexure. For the purpose of our theoretical analysis, the structure is replaced by a model consisting of numerous two-dimensional rectangular units and it is analysed for stresses and vibration frequency by the method of finite element.

### RESUME

Les treize maitresses-planchers de cet immeuble de bureaux d'un plan de 108 x 108 pieds sont suspendus par câbles ancrés au noyau central en béton armé qui mesure 36 x 36 pieds en plan et 265 pieds en hauteur. La petite surface de fondation et l'effet de la précontrainte des charges rendent cet immeuble très résistant aux tremblements de terre et aux fléchissements. Pour l'analyse théorique la structure est remplacée par un modèle composé de rectangles bidimensionnelles. L'analyse des tensions et des vibrations est opérée par la méthode des éléments finis.

## ZUSAMMENFASSUNG

Die dreizehn Hauptdecken dieses Bürohauses mit einem Grundriss von 108 x 108 Fuss hängen an Kabeln, die im Stahlbetonkern verankert sind, der im Grundriss 36 x 36 Fuss und in der Höhe 265 Fuss misst. Die kleine Gründungsfläche sowie die Vorspannwirkung der Lasten machen dieses Gebäude sehr widerstandsfähig gegenüber Erdbeben und Biegung. Für die theoretische Untersuchung wird das Gebäude durch ein Modell ersetzt, welches aus zweidimensionalen Rechtecken zusammengesetzt ist. Die Spannungs- und Schwingungsberechnung erfolgt nach der Methode der endlichen Elemente.



Fig. 1

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## DISCUSSION LIBRE • FREIE DISKUSSION • FREE DISCUSSION

Discussion of Paper Entitled "Dynamic Design of High-Rise Building subjected to Wind and Seismic Loads" by Kawamura and Others

Discussion du travail intitulé "Projet d'une structure élevée soumise aux charges dynamiques du vent et des séismes" de Kawamura et autres

Diskussion zum Beitrag "Entwurf eines Hochbaues unter Berücksichtigung von dynamischen Wind- und Erdbebenkräften" von Kawamura und anderen

D.V. REDDY  
Dr.-Ing.  
Memorial University  
St. John's, Newfoundland  
Canada

I would like to make the following comments:-

1) Validity of the Lumped Mass Approximation

It is important to consider the distributed nature of the mass by considering the framed structure in its actual form. Warburton (1) has pointed out that replacing the mass of the vertical members by lumped masses at the ends of the members and neglecting the flexibility of the horizontal members can lead to large errors in the case of multi-storey frames.

2) Influence of Layout

Shepherd and Donald (2) have shown that torsional vibration becomes important for asymmetric layouts making the lumped mass approximation very unsatisfactory. The floors of a building will undergo both translational and rotational movement and even in a purely symmetrical building, like the one considered by the authors, the slightest change in the distribution of mass or stiffness is enough to give such a structure the characteristics of an unbalanced building.

3) Errors

In dynamic analysis the check on frequencies is not adequate as the stresses are much more important.

## BIBLIOGRAPHY

- (1) Warburton, G.B., 'The Dynamical Behaviour of Structures', Pergamon Press, Gt. Britain, 1964, pp. 165-166.
- (2) Shepherd, R. and Donald, R.A.H., 'Seismic Response of Torsionally Unbalanced Buildings', Journal of Sound and Vibration, Vol. 6, No. 1, 1967, pp. 20-37.

## SUMMARY

The effect of the distributed nature of the mass and the influence of the layout in multi-storey frames are discussed. The lumped mass approximation is criticised and the possibility of torsional vibration, even in buildings with symmetric geometrical layouts due to changes in the distribution of mass or stiffness, is indicated.

## RESUME

On discute ici l'effet de la nature étendue de la masse et l'influence de l'agencement dans les portiques à étages multiples. L'auteur critique l'approximation de la masse totale et indique la possibilité d'existence de vibrations de torsion, même pour des bâtiments à disposition géométrique symétrique, dues au changement dans la distribution de la masse ou de la rigidité.

## ZUSAMMENFASSUNG

Es wird die Auswirkung der verschieden verteilten Natur der Masse und der Einfluss beim Entwurf mehrstöckiger Bauten diskutiert. Die globale Massenannäherung wird kritisch beleuchtet und die Möglichkeit von Torsionsschwingungen, selbst in Bauten mit symmetrisch geometrischen Entwürfen infolge des Wechsels in der Massen- und Steifigkeitsverteilung angegeben.



**Bemerkungen des Verfassers des Einführungsberichtes**  
Comments by the Author of the Introductory Report  
Remarques de l'auteur du rapport introductif

FRITZ LEONHARDT  
BRD

Die Beiträge zeigen, dass bei Hochhäusern die Kombination eines Kernes mit dem aus perforierten Aussenwänden gebildeten vertikalen Kastenträger (Rohr) für schlanke Hochhäuser zur Aufnahme der Windkräfte zunehmende Bedeutung erlangt. Es handelt sich dabei zweifellos um eine technisch und wirtschaftlich günstige Lösung. Es ist zu begrüßen, dass sich Coull und Subedi um eine vereinfachte Näherungsberechnung dieser komplizierten räumlichen Tragwerke bemüht haben und deren Genauigkeitsgrad durch einen Modellversuch aufzeigten.

Den wertvollsten Beitrag zum Verhalten solcher Hüllrohr-Kern-Hochhäuser (Hull-Core Structures) lieferten zweifellos Kawamura und Mitarbeiter durch die dynamische Behandlung des KTC-Hochhauses in Kobe für Erdbebenkräfte und Wind. Es ist sehr verdienstvoll, dass an diesem Hochhaus umfangreiche Versuche und Messungen durchgeführt wurden und dass das dynamische Verhalten eines solchen Hochhauses im Film so anschaulich dargestellt wurde. Die Übereinstimmung zwischen Rechnung und Messung hinsichtlich der Schwingungsfrequenzen ist beachtlich gut. Erwünscht wären weitere Angaben über die Dämpfung und vor allem weitere Beobachtungen und Messungen über das Verhalten dieses Hochhauses bei Wind. Es besteht heute kein Zweifel mehr darüber, dass wir die hohen, schlanken Bauwerke nach ihrem dynamischen Verhalten berechnen und bemessen müssen, weil die quasi statische Betrachtung in der Regel eine viel zu hohe Sicherheit und damit eine Verschwendung von Baustoffen ergibt. Zur Entwicklung der dynamischen Berechnungsmethoden brauchen wir aber Messungen an Bauwerken, um einerseits die Struktur des Windes und andererseits die Antwort der Bauwerke auf den Windangriff zu kennen. Bisherige Messungen zeigten, dass die Ausbiegungen hoher, schlanker Bauwerke nur 25 bis 35 % der quasi statisch für die gemessenen maximalen Windgeschwindigkeiten berechneten



Werte erreichen. Die Ursachen dieser grossen Abweichung der Berechnung von der Wirklichkeit müssen dringend geklärt werden. Ich vermute, dass die Böen eine nur so kurze Dauer haben, dass ihre Energie nicht ausreicht, um die bei einer länger wirkenden Last entstehende Durchbiegung zu erzeugen. Diese Fragen können nur durch Messungen an Bauwerken weiter geklärt werden.

In dem Beitrag von Ukeguchi und Mitarbeitern halte ich den erneuten Hinweis für wichtig, dass die Umgebung der Bauwerke und ihr Einfluss auf die Windströmung, insbesondere auf die Turbulenz von grosser Bedeutung sind, so dass stählerne Schornsteine an einer Stelle schwingen, während die gleichen Schornsteine an einem anderen Ort stabil sind. Erneut zeigt sich auch die dämpfende Wirkung von wendelartig um Schornsteinrohre gelegte Drahtseile, die mit der Scruton-Wendel vergleichbar sind.

Der Bericht über das Schwingungsverhalten des stählernen Fachwerkturnes am Strand von Hawai zeigte, dass wir für diese rechnerisch leicht erfassbaren Tragwerke die Schwingungen heute sehr präzise vorausberechnen können.

Der für uns Europäer befremdend wirkende Peace Tower in Osaka muss als eine Skulptur japanischer Prägung und Kunstvorstellung betrachtet werden. Es ist beachtlich, wie gründlich sein Verhalten bei Erdbeben und Wind durch grosse Modellversuche untersucht wurde. Das Rissverhalten dieses Bauwerkes wird allerdings mehr von Temperaturspannungen abhängen als von Lastspannungen durch Wind oder durch mässige Erdbeben.

Zu den Berichten über das West Coast Transmission Building in Vancouver möchte ich nur sagen, dass bei derartig einfachen Kerntürmen die Berechnungsmethoden vielleicht weniger wichtig sind als die sorgfältige Durchbildung der konstruktiven Details. Den Lichtbildern war zu entnehmen, dass z. B. der Korrosionsschutz an Klemmstellen der Hängeseile für die Sicherheit eines solchen Bauwerkes wichtig ist.

Von besonderer Bedeutung erscheint mir der Beitrag von Miyata und Ito, der in Fortsetzung der Arbeiten von Davenport sich mit der Wirkung von Böen bei unterschiedlicher Turbulenz auf biegsame, schlanke Bauwerke (z. B. Türme oder Hängebrücken) beschäftigt. Gerade solche Arbeiten müssen aber durch Messungen an ausgeführten Bauwerken im natürlichen Wind überprüft werden, wie dies zum Beispiel durch Messungen an der Golden Gate Brücke geschieht.

Wenn ich meinen Einführungsbericht zu diesem Thema betrachte, in dem ich auf vielerlei Probleme der hohen, schlanken Bauwerke hingewiesen habe, so sind die Beiträge mit Ausnahme der japanischen Arbeiten enttäuschend. Die Europäer fehlen fast ganz, obwohl doch auch in Europa viele hohe, schlanke Bauwerke errichtet werden. Wichtige Probleme, wie zum Beispiel die Sicherheit von Stahlbetontürmen unter Beachtung der Deformationen im Zustand II oder die Gründungen oder Entwurfskriterien für das Wohlbefinden der Menschen in Hochhäusern wurden überhaupt nicht

angesprochen. Es wäre erwünscht, dass sich besonders die europäischen Ingenieure um die Klärung solcher Fragen bemühen und Beiträge liefern. Es ist zu hoffen, dass die von Professor Beedle so wirkungsvoll geplante internationale Konferenz über ' Tall Buildings ', die im August dieses Jahres an der Lehigh University in Bethlehem, Pennsylvania, stattfinden soll, bessere Erträge auch über die hohen, schlanken Bauwerke erbringt. Man darf dieser Konferenz, die gemeinsam von IVBH und ASCE durchgeführt wird, und die alle Aspekte der grossen und hohen Bauwerke behandeln will, mit Interesse entgegensehen und guten Erfolg wünschen.

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## IV/V

### **Conclusions to themes IV and V**

Conclusions aux thèmes IV et V

Schlussfolgerungen zu Thema IV und V

### **GEORG WÄSTLUND**

President of Working Commission III

Sweden

Working Commission III has been responsible for themes IV and V, i.e.

IV. Interrelation between Design and Methods of Construction  
for elevated Highways and Viaducts.

V. Tall slender Structures.

For theme IV there were two introductory reports, one by Prof. Menn and one by Prof. van der Vlugt. There were 7 contributions to the prepared discussion and 8 to the free discussion.

For theme V there was one introductory report, i.e. by Prof. Leonhardt. To the prepared discussion there were 8 contributions, but to the free discussion only one.

Prof. van der Vlugt summed up the discussion-contributions for theme IV, saying that they were of high quality, very informative, and very well illustrated by slides. They had brought new ideas and new applications, e.g. about erection methods for flyovers of railways under full traffic. He also pointed out some items for further research in future.

One contribution should perhaps be mentioned particularly, i.e. the one by Prof. Menn. He showed a diagram over material-economy of executed bridges, in Switzerland, Germany and France, showing the relation between amount of material, concrete and steel, and bridge span length. This relation had a very small scatter, only about 5%.

For theme V Prof. Leonhardt pointed out, that there were very interesting reports, mainly from Japan, but no one from Europe. Those reports showed a very good agreement between measured oscillations of tall towers and calculated oscillations. He meant that such measurements were most valuable, and that more research in that field was desirable. He pointed out, that such research also ought to be made in Europe.

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