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Autor(en): Purzitsky, N.<br>Objekttyp: Article<br>Zeitschrift: Commentarii Mathematici Helvetici

Band (Jahr): 55 (1980)
PDF erstellt am:
30.06.2024

Persistenter Link: https://doi.org/10.5169/seals-42370

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# On Tsuji's and Pommerenke's examples for fuchsian groups of convergence type 

N. Purzitsky

## Introduction

Let $\Gamma$ be an infinitely generated fuchsian group acting on the unit disc $\Delta$ and $\Omega$ the set of ordinary points of $\Gamma$ in the complex plane $\varnothing$. In this paper we will consider only those groups $\Gamma$ for which $\Omega \cap \partial \Delta=\varnothing$, where $\partial \Delta$ is the boundary of $\Delta$ and $\varnothing$ is the empty set. The classical problem to which this paper has relevance is the problem of determining the divergence or convergence of the series

$$
\left(\begin{array}{c}
\left.\sum_{\substack{c \\
c \neq 0^{*}}}\right)_{i r} \\
\frac{1}{|c|^{2}} .
\end{array}\right.
$$

This problem appears in [1, p. 176 and 6, p. 515]. This series is known to converge [6, p. 514] if the Lebesgue linear measure of the some fundamental domain $D$ of $\Gamma$ intersect $\partial \Delta$ is positive. Is the converse true?

No, in [6, p. 515] counterexamples for which $m\left(\bar{D}_{0} \cap \partial \Delta\right)=0$ are given, where $m(S)$ is the Lebesgue linear measure in $\partial \Delta, D_{0}$ is the Ford fundamental domain, and $\bar{D}_{0}$ is the closure of $D_{0}$. Although these examples are probably correct, there was a significant gap in Tsuji's claim that his constructions provide examples to anything at all. In particular, it is not obvious that if $m\left(\bar{D}_{0} \cap \partial \Delta\right)=0$, then $m(\bar{D} \cap \partial \Delta)=0$ for all other fundamental polygons of $\Gamma$. This gap was filled by Pommerenke in [3], where he gives examples of his own. Actually Pommerenke proves that in fact if $\Gamma$ is of convergence type, i.e. $\sum 1 /|c|^{2}<\infty$, and $m\left(\bar{D}_{0} \cap \partial \Delta\right)=$ 0 , then for any Borel subset $B$ of $\partial \Delta$ for which $V(B) \cap B=\varnothing$, if $V$ is not the identity transformation, we have $m(B)=0$.

The confusion to the validity or completeness of the Tsuji examples apparently stems from the notion that if $m(\bar{D} \cap \partial \Delta)=0$ for one fundamental polygon of $\Gamma$ then $m\left(\bar{D}^{\prime} \cap \partial \Delta\right)=0$ for all other fundamental polygons $D^{\prime}$ of $\Gamma$. In [4] examples are given to show that this notion is false. The theorem proved in this paper is an extension of these examples to all groups $\Gamma$ for which $\Omega \cap \partial \Delta=\varnothing$.

THE MAIN THEOREM 1. Let $\Gamma$ be an infinitely generated fuchsian group for which $\Omega \cap \partial \Delta=\varnothing$. Then $\Gamma$ has a fundamental polygon $P$ such that $m(\bar{P} \cap \partial \Delta)=0$.

Remarks. It will be evident that the above theorem is true for any function $m^{*}: \beta \rightarrow[0, \infty)$, where $\beta$ is the set of Borel subsets of $\partial \Delta$, such that:
(a) $m^{*}(A \cup B) \leq m^{*}(A)+m^{*}(B)$;
(b) if $A \subseteq B$, then $m^{*}(A) \leq m^{*}(B)$;
(c) for each $\varepsilon>0$ there exists a $\delta>0$ such that $m\left(\left\{e^{i \theta}: \theta_{0}-\delta<\theta<\theta_{0}+\delta\right\}\right)<\varepsilon$ for all $\theta_{0}$.

Preliminaries. We use the following two theorems.

THEOREM 2. Let $\left\{C_{i}, C_{i}^{\prime}\right\}_{i}$ be a collection of circles perpendicular to $\partial \Delta$ which satisfy: (*) all circles are exterior or externally tangent to each other except for the possibility that $C_{i} \cap C_{i}^{\prime} \cap \Delta \neq \varnothing$ in the special case mentioned below. Let $\Gamma$ be a fuchsian group and $A_{i} \in \Gamma$ be such that $A_{i}\left(C_{i}\right)=C_{i}^{\prime}$ with the outside of $C_{i}$ going onto the inside of $C_{i}^{\prime}$. If $A_{i}$ is elliptic, then we assume $A_{i}$ is of minimal rotation, i.e. $\left|\operatorname{tr}\left(A_{i}\right)\right|=2 \cos (\pi / n)$ for some $n$, and that $C_{i} \cap C_{i}^{\prime} \cap \Delta$ is the fixed point of $A_{i}$, if $n \neq 2$. If $n=2$, then $C_{i}=C_{i}^{\prime}$. Then the polygon $P$ formed by the intersection of $\Delta$ with the region exterior to all the circles from $\left\{C_{i}, C_{i}^{\prime}\right\}_{i}$ is a fundamental polygon of $\Gamma$ if and only if
(1) the group generated by the $\left\{A_{i}\right\}_{i=1}^{\infty}$, denoted by $\left\langle A_{1}, A_{2}, \ldots\right\rangle$ is $\Gamma$ and
(2) $\Omega \cap \partial \Delta=\varnothing$ or $\bar{P}$ contains a fundamental set of $\Omega \cap \partial \Delta$.

Theorem 2 is proven in [5].
The next theorem is a special case of Theorem 6 in [4].

THEOREM 3. Every infinitely generated group for which $\Omega \cap \partial \Delta=\varnothing$ has a Schottky fundamental domain $P$ such that for each $A \in S(P)$ we have that $A$ is either a handle generator, an ideal boundary generator, a parabolic transformation, an elliptic transformation, or a free hyperbolic element.

We need to define some of the terms of Theorem 3. A handle generator $X \in \Gamma$ is a hyperbolic transformation which identifies a pair of sides of $P$ for which there is another hyperbolic generator $Y$, also identifying a pair of sides of $P$, such that $C_{X} \cup C_{Y} \cup C_{X}^{\prime} \cup C_{Y}^{\prime}$ is expressable as a Jordan arc, where $C_{T}$ and $C_{T}^{\prime}=T\left(C_{T}\right)$ are sides of $P$ identified by $T$. Note here that the axes of $X$ and $Y$ intersect.

An ideal boundary generator is a hyperbolic transformation which identifies a
pair of sides whose axis does not intersect the axis of any other hyperbolic transformation identifying a pair of sides of $P$.

A Schottky fundamental polygon of $\Gamma$ is a hyperbolic convex region $D$ in $\Delta$ which is the exterior of circles which satisfy (*) such that $\Delta=U_{V \in \Gamma} V(\bar{D})$ and $V(D) \cap D=\varnothing$ for all $V \in \Gamma, V \neq\left(\begin{array}{ll}1 & 0 \\ 0 & 1\end{array}\right)$.

Cutting and Pasting. For the precise definition of cutting and pasting we refer to [1, p. 242]. We should say, however, that in this paper we will cut and paste only Schottky fundamental polygons and in such a way as to obtain only other Schottky fundamental polygons. With this restriction a rough definition of a cut and paste is the following. We draw a geodesic in $P$, say $g$, in such a way that $P \backslash g$ has two connected components, say $R_{1}$ and $R_{2}$. We let $A \in \Gamma$ pair the sides $C_{A}$ and $C_{A}^{\prime}=A\left(C_{A}\right)$ of $P$. We assume $g$ is drawn so that $C_{A} \subseteq \bar{R}_{1}$ and $C_{A}^{\prime} \subseteq \bar{R}_{2}$. Then a cut and paste by A along $g$ is the new polygon $P_{1}=\left[R_{2} \cup A\left(\bar{R}_{1}\right)\right]^{0}$, where $S^{0}$ is the interior of $S$. To insure $P_{1}$ is a Schottky polygon we choose $g$ so that either both endpoints of $g$ are in $\partial \Delta$, if $A$ is not elliptic, or one endpoint of $g$ is the elliptic fixed point of $A$, in the case $A$ is elliptic.

Remark. Let the sides of $P$ be labelled and enumerated by the sequence $\left\{C_{i}, C_{i}^{\prime}\right\}_{i=1}^{\infty}$, where $C_{i}^{\prime}=A_{i}\left(C_{i}\right)$ for some $A_{i} \in \Gamma$. Let $S(P)=\left\{A_{1}, A_{2}, \ldots\right\}$. We note $S\left(P_{1}\right)=\left\{A^{\varepsilon_{x}} X A^{\delta_{x}}: \varepsilon_{X}, \delta_{X}=0, \pm 1, \varepsilon_{A}=\delta_{A}=0\right.$, and $\left.X \in S(P)\right\}$. The change of $S(P)$ to $S\left(P_{1}\right)$ is called a Nielsen transformation. It is classical [2] that $\langle S(P)\rangle=$ $\left\langle S\left(P_{1}\right)\right\rangle$.

We now describe three ways of cutting and pasting a Schottky polygon $P$ to a new Schottky polygon $P_{1}$. When we say below to cut and paste $P$ to say $P_{1}$, we shall mean that: starting with $P$ perform one of the three operations described below depending on $X$ to obtain $P_{1}$. Note that in the type 3 cutting and pasting we also prescribe the number $\varepsilon$.

Type 1. Let $A$ be either an elliptic or parabolic transformation (by assumption there are no free hyperbolic generators) and $x \in \partial \Delta \cap \bar{P}$. Let $g$ be the geodesic joining $x$ to the fixed point of $A$. The type 1 cut and paste is the cutting and pasting of $P$ along $g$ by $A$.

Type 2. If $A$ is a handle generator and $x \in \partial \Delta \cap \bar{P}$, then we need four cuts and pastes. We assume that as one walks $\partial \Delta$ counterclockwise one encounters the sets $\{x\}, C_{\mathrm{A}} \cap \partial \Delta, C_{\mathrm{B}} \cap \partial \Delta, C_{\mathrm{A}}^{\prime} \cap \partial \Delta, C_{B}^{\prime} \cap \partial \Delta$, respectively. Draw $\mathrm{g}_{\mathrm{A}}$ from $x$ to the endpoint of $C_{\mathrm{A}}$ for which $C_{\mathrm{A}} \cap \Delta$ is in one component of $\Delta \backslash g_{\mathrm{A}}=R_{1} \cup R_{2}$, say $R_{1}$, and $C_{B} \cap \Delta, C_{A}^{\prime} \cap \Delta, C_{B}^{\prime} \cap \Delta$ are all in $R_{2}$. Cut along $g_{A}$ and glue $A\left(R_{1}\right)$ to $R_{2}$ along $C_{A}^{\prime}$. Repeat this procedure in succession for $C_{B}^{\prime}$ and $A(x), g_{A}^{\prime}=A\left(g_{A}\right)$ and $B^{-1} A(x), g_{B}=B^{-1}\left(g_{B^{-1}}\right)$ and $A^{-1} B^{-1} A(x)$. In the resulting polygon the sides which are paired by $A$ and $B$ all have both endpoints equivalent to $x$.

Type 3. Let $A$ be an ideal boundary generator $x \in \partial P \cap \partial \Delta, \varepsilon>0$ and $x_{A}, y_{A}$ be the fixed points of $A$. We first observe that there exists a $\delta>0$ such that $|A(z)-z|<\varepsilon$ if either $\left|z-y_{A}\right|<\delta$ or $\left|z-x_{A}\right|<\delta$. Let $C_{A}, C_{A}^{\prime}=A\left(C_{A}\right)$ be the sides of $P$, a Schottky polygon, which are paired by $A$. Let $x_{A}$ be inside the circle determined by $C_{A}^{\prime}$ and let $w$ be the endpoint of $C_{A}$ which lies in the connected component of $\partial \Delta \backslash\left\{x_{A}, y_{A}\right\}$ which does not contain $x$. Let $g_{1}$ be the geodesic joining $x$ to $w$. Cut $P$ along $g_{1}$ and paste along $C_{A}^{\prime}$ to obtain a new polygon $P_{1}$. If $\left|A(w)-A^{2}(w)\right|<\varepsilon$, we stop. If not repeat this procedure. By the above remarks, since $\lim _{n \rightarrow \infty} A^{n}(w)=x_{A}$, we see that after finitely many applications we do indeed obtain a fundamental polygon for which a pair of the equivalent endpoints, $w_{1}, w_{2}=A\left(w_{1}\right)$, of the sides identified by $A$ are within $\varepsilon$ of each other. Since the minor arc determined by $w_{1}, w_{2}$ has length $\theta=2 \arcsin \left[\left|w_{1}-w_{2}\right| / 2\right]$ we see that $\theta$ can be made arbitrarily small by this cut and paste.

Proof of the Main Theorem. We start with the fundamental domain $P$ of Theorem 3. We let $\left\{s_{i}, s_{i}^{\prime}\right\}_{i=0}^{\infty}$ be the sides of $P$ enumerated so that $s_{i}^{\prime}=A_{i}\left(s_{i}\right)$ for some $A_{i} \in \Gamma$. We set $S(P)=\left\{A_{i}\right\}_{i=0}^{\infty}$. We assume that $m=m(\bar{P} \cap \partial \Delta)>0$, otherwise we take $P$ as our fundamental domain. We also assume that -1 is an endpoint of $s_{0}$ and $1=A_{0}(-1)$ is the endpoint of $s_{0}^{\prime}$ equivalent to -1 . If $A_{0}$ is a handle generator we let $A_{j_{0}}$ be the member of $S(P)$ whose axis intersects the axis of $A_{0}$. Set $S_{0}=\left\{A_{0}\right\}$, if $A_{0}$ is not a handle generator, or $S_{0}=\left\{A_{0}, A_{j_{0}}\right\}$, if $A_{0}$ is a handle generator.

We do the case that $A_{0}$ is not an ideal boundary generator. This means that the sides of $P$ paired by the elements of $S(P) \backslash S_{0}$ lie in either $\bar{H}^{+}=\{x+i y: y \geqq 0\}$ or $\bar{H}^{-}=\{x+i y: y \leqq 0\}$; say $\bar{H}^{+}$. In the general case the proof given below would be repeated for the sides which lie in $\bar{H}^{-}$.

We let $i_{1}$ be the least positive integer among the indices of $S(P) \backslash S_{0}$. We choose $x=1$ and cut and paste, as dictated by the type of generator $A_{i_{1}}$ is, in such a way that 0 is in the resulting polygon $P_{1}$. We set $S_{1}=S_{0} \cup\left\{A_{i_{1}}\right\}$, if $A_{i_{1}}$ is not a handle generator. If $A_{i_{1}}$ is a handle generator, then we set $S_{1}=S_{0} \cup\left\{A_{i_{1}}, A_{j_{1}}\right\}$, where $A_{j_{1}}$ is the unique element of $S(P)$ whose axis intersects the axis of $A_{i_{1}}$. Let $T_{1}$ be the set of circles determined by the sides of $P_{1}$ which are paired by elements of $S_{1}$. If $A_{i_{1}}$ is an ideal boundary generator than we choose $\varepsilon_{i_{1}}=\frac{1}{2}$ in the type 3 cut and paste.

We next endow $S\left(P_{1}\right)$ with the enumeration derived from $S(P)$. This is best described by observing that each $Y \in S\left(P_{1}\right)$ is of the form $Y=W A_{j} V$, where $W, V \in\left\langle S_{1}\right\rangle$. We index $Y$ by $j$ and write $S\left(P_{1}\right)=\left\{A_{0}=Y_{0}, Y_{1}, \ldots, A_{i_{0}}=Y_{i_{0}}, \ldots\right\}$, where $Y_{j}=W A_{j} V$ for some $A_{j} \in S(P)$.

We continue inductively. Given $n \geq 1, P_{n}, S_{n}, T_{n}$ we enumerate $S\left(P_{n}\right)=$ $\left\{X_{0}=A_{0}, X_{1}, \ldots\right\}$ by the enumeration derived from $S\left(P_{n-1}\right)$. We note that if $S_{n}$
contains precisely $k_{n}$ ideal boundary generators then $J_{n}=\partial \Delta \cap \operatorname{Ext}\left(T_{n}\right)$, where Ext $\left(T_{n}\right)$ is the closed region outside all the circles determined by the sides of $P_{n}$ in $T_{n}$, has $k_{n}+1$ connected components, $J_{1, n}, \ldots J_{k_{n}+1, n}$ all of which are in $\bar{H}^{+} \cap \partial \Delta$.

Now for each component $J_{r, n}$ let $S\left(P_{n}\right)_{r}=\left\{X \in S\left(P_{n}\right) \backslash S_{n}: C_{X} \cap J_{r, n} \neq \varnothing\right\}$, where $C_{X}, C_{X}^{\prime}=X\left(C_{X}\right)$ are the sides of $P_{n}$ paired by $X$. We see that from the way we cut and the definition of boundary generator, that $C_{X}^{\prime} \cap J_{r, n} \neq \varnothing$ if and only if $C_{X} \cap J_{r, n} \neq \varnothing$. We let $i_{r, n}$ be the least positive index among the indices of $S\left(P_{n}\right)_{r}$ and $x_{r}$ the endpoint of $J_{r, n}$ closest to 1 . We now cut and paste $P_{n}$ by $X_{i_{1, n}}$ to $P_{1, n}$ and then for $j=1,2, \ldots, k_{n}$ in succession we cut and paste $P_{j, n}$ by $X_{i, n}$ to $P_{j+1, n}$ and finally $P_{k_{n}, n}$ is cut and pasted by $X_{i_{k_{n}+1, n}}$ to $P_{n+1}$. By our assumption on $\pm 1$ and $s_{0}, s_{0}^{\prime}$ all geodesics drawn in the cutting and pasting have 0 outside the circle determined by them. Therefore we can and do choose all cuts and pastes so that $0 \in \cap_{n=1}^{\infty} P_{n}$. Naturally the type of cut and paste used in each step will be determined by the type of generator $X_{i, n}$ is. In the case $X_{i, n}$ is an ideal boundary generator we choose $\varepsilon_{i, n}=1 /\left(k_{n}+1\right) 2^{n}$.

To complete the induction we set $S_{n+1}=S_{n} \cup\left\{X_{i_{1, n}}, \ldots, X_{i_{r, n}}, X_{j_{r, n}}, \ldots, X_{i_{k_{n}+1, n}}\right\}$ and $T_{n+1}$ to be the circles determined by the sides paired by elements of $S_{n+1}$. Now set $S=\cup_{n=1}^{\infty} S_{n}, T=\cup_{n=1}^{\infty} T_{n}$. We note that if the index $j$ has an element $X_{j} \in S_{n}$, then $A_{j}=W X_{j} V$ for some $W, V \in\left\langle S_{n}\right\rangle$ is in $\left\langle S_{n}\right\rangle$ and hence $A_{j} \in\langle S\rangle$. Since each $P_{n}$ and $P_{r, n}$ is a Schottky polygon each $j$ has such an $X_{j}$. For the only way we could miss setting $i_{r, n}=j$ for some $r, n$ is that the index $j$ vanished from $S\left(P_{n}\right)=\left\{X_{0}, \ldots\right\}$. This would mean that if $S\left(P_{n-1}\right)=\left\{Y_{0}, Y_{1}, \ldots\right\}$, then $W Y_{j} V=I$ for some $W, V \in\left\langle S_{n}\right\rangle$ and $Y_{j} \notin S_{n}$, and this is not possible. Thus $\langle S\rangle=\Gamma$. It is also clear 0 is outside all the circles $C \in T$. So by Theorems 2 , the region $P^{\prime}$ exterior to all the $C \in T$ is a fundamental region of $\Gamma$.

It remains to show $m\left(\bar{P}^{\prime} \cap \partial \Delta\right)=0$. We show that for any $\varepsilon>0, m\left(\bar{P}^{\prime} \cap \partial \Delta\right)<\varepsilon$. We let $\varepsilon>0$ and choose $N$ such that $\sum_{j=N}^{\infty} 1 / 2^{j}<\varepsilon / 2$; then $\varepsilon / 2>1 / 2^{N}$. We consider $P_{N}$. Let $J_{1, N}, \ldots, J_{k_{N}+1, N}$ be, as before, the connected components of $\partial \Delta$ outside the circles from $T_{N}$. Since $\Omega \cap \partial \Delta=\varnothing$, for each $r=1,2, \ldots, k_{N}+1$ there exists $N_{r}>N$ such that $\max \left\{m\left(J_{t, N_{r}} \cap J_{r, N}\right): t=1,2, \ldots, k_{N_{r}}+1\right\}<\varepsilon / 2\left(k_{N}+1\right)$. Let $N^{\prime}=$ $\operatorname{Max}\left\{N_{1}, N_{2}, \ldots, N_{k_{N+1}}\right\}$. We observe that, if $k_{N^{\prime}}>k_{N}$, there are at most $k_{j}+1$, $j=N, N+1, \ldots, N^{\prime}-1, J_{r, N^{\prime}}$ for which

$$
C_{j}=\frac{1}{\left(k_{j}+1\right) 2^{j}} \geqq m\left(J_{r, N^{\prime}}\right)>C_{j+1}=\frac{1}{\left(k_{j+1}+1\right) 2^{j+1}}
$$

and there are at most $\left(k_{N}+1\right) J_{r, N^{\prime}}$ such that

$$
C_{N}=\frac{1}{\left(k_{N}+1\right)} \frac{1}{2^{N}} \leqq m\left(J_{r, N^{\prime}}\right) \leqq \frac{\varepsilon}{2\left(k_{N}+1\right)}=d, \quad \text { since } \quad \varepsilon \geqq \frac{1}{2^{N-1}} .
$$

This follows from our choice of the " $\varepsilon$ " in the type 3 cutting and pasting. Hence,

$$
\begin{aligned}
m\left(\partial \Delta \cap P^{\prime}\right) \leqq & \sum_{r=1}^{k_{N^{\prime}}+1} m\left(J_{r, N^{\prime}}\right)=\sum_{j=N}^{N^{\prime}-1} \sum_{C_{1+1}<m\left(J_{r, N^{\prime}}\right) \leqq C_{1}} m\left(J_{r, N^{\prime}}\right) \\
& +\sum_{m\left(J_{\left.r, N^{\prime}\right)} \leq C_{N^{\prime}}\right.} m\left(J_{r, N^{\prime}}\right)+\sum_{C_{N} \leqq m\left(J_{r, N^{\prime}}\right) \leqq d} m\left(J_{r, N^{\prime}}\right) \\
\leqq & \sum_{j=N}^{N^{\prime}} \frac{1}{2^{j}}+\frac{\varepsilon}{2}=\frac{\varepsilon}{2}+\frac{\varepsilon}{2}=\varepsilon .
\end{aligned}
$$

## REFERENCES

[1] Lehner, J., Discontinuous groups and automorphic functions, AMS Surveys No. 8, Providence, R.I., 1964.
[2] Magnus, W., Karrass, A., Solitar, D., Combinatorial groups theory, Wiley Interscience Publishers, New York, 1966.
[3] Pommerenke, Ch., On the Green's function of fuchsian groups, Ann. Acad. Sci. Fennicae, Ser. A I Math. 2, 409-427 (1976).
[4] Purzitsky, N., Fricke polygons for infinitely generated groups I. (to appear).
[5] -, A cutting and pasting of infinite sided polygons with applications to fuchsian groups. (to appear Acta Mathematica).
[6]. Tsusi, M., Potential Theory, Chelsea, New York, 1959.
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Received June 29, 1979

