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**Artikel:** ON CONNES' JOINT DISTRIBUTION TRICK AND A NOTION OF AMENABILITY FOR POSITIVE MAPS  
**Autor:** POPA, Sorin

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“Sur certaines propriétés spectrales du laplacien sur les graphes”, University Paul Sabatier, Toulouse, thesis 1996). He proved this result by using different methods than ours. Note that Zuk’s result generalized (unknowingly!) our previous similar statement which only covered the particular graphs coming from subfactors ([Po2,3,4]). On the other hand, our Corollary 0.2 in the present paper proves (by using Connes’ distribution trick) an equivalence between Kesten and Følner type amenability conditions that is sensibly more general than all these prior results.

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Sorin Popa

Université de Genève

Section de Mathématiques

Case postale 240

CH-1211 Genève 24

Switzerland

*e-mail*: Sorin.Popa@math.unige.ch