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## IDEAL SOLUTIONS OF THE TARRY-ESCOTT PROBLEM OF DEGREE FOUR AND A RELATED DIOPHANTINE SYSTEM

by Ajai CHOUDHRY

ABSTRACT. In this paper, the complete ideal symmetric solution in integers of the Tarry-Escott problem of degree four, that is, of the system of simultaneous equations  $\sum_{i=1}^s a_i^r = \sum_{i=1}^s b_i^r$ ,  $r = 1, 2, 3, 4$ , has been obtained. In addition, a parametric ideal non-symmetric solution has also been obtained, and this non-symmetric solution has been used to obtain a parametric solution of the diophantine system  $\sum_{i=1}^s a_i^r = \sum_{i=1}^s b_i^r$ ,  $r = 1, 2, 3, 4$  and 6.

### 1. INTRODUCTION

The Tarry-Escott problem of degree  $k$  consists of finding two sets of integers  $a_1, a_2, \dots, a_s$  and  $b_1, b_2, \dots, b_s$  such that

$$(1) \quad \sum_{i=1}^s a_i^r = \sum_{i=1}^s b_i^r, \quad r = 1, 2, \dots, k.$$

There is a well-known theorem [6, p.614] due to Frolov according to which the relations (1) imply that

$$(2) \quad \sum_{i=1}^s (Ma_i + K)^r = \sum_{i=1}^s (Mb_i + K)^r, \quad r = 1, 2, \dots, k,$$

where  $M$  and  $K$  are arbitrary integers. That is, if  $(a_1, a_2, \dots, a_s; b_1, b_2, \dots, b_s)$  is a solution of the system (1), then

$$(Ma_1 + K, \dots, Ma_s + K; Mb_1 + K, \dots, Mb_s + K)$$

is also a solution of (1). This theorem is easily established by using the binomial theorem. If one solution of the system (1) is obtained from another through