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Analysis of Alpine glacier length change records with a macroscopic glacier model

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1 Introduction

The record of glacier length changes in the Swiss Alps, measured during the last century (GLACIOLOGICAL REPORTS 2009), is unique in its length, its spatial coverage and its variety of glacier geometries. The collective data set contains a wealth of information about past changes in glacier mass balance, and thus climate, albeit in an indirect manner. These data can be viewed as a set of sensors probing climate, where each sensor has a different response to the external forcing.

The position of a glacier terminus depends on two processes: advection of ice into the terminus area, and melting of ice at the surface. If both processes are of the same magnitude, the glacier terminus geometry remains unchanged. Upon a sudden change in mass balance, the terminus geometry reacts immediately due to increased or decreased melting, and with some delay until glacier dynamics changes the mass transport into the terminus area (e.g. NYE 1963). For an oscillating climate, this delay in response depends on the frequency of the mass balance changes, and can be out of phase for frequencies lower than the volume time scale (HUTTER 1983; LÜTHI 2009; NYE 1965a).

Several studies have used glacier length changes to infer climate history (e.g. KLOK & OERLEMANS 2003; NYE 1965b; OERLEMANS 2001; OERLEMANS 2005). STEINER et al. (2005) and STEINER et al. (2008) used reconstructed climate data to drive a neural network trained on a glacier length record to analyze length changes, to infer climate sensitivity, and to predict the future evolution of several glaciers. The studies by HARRISON et al. (2003) and OERLEMANS (2007) are quite similar in scope to the present study, although with different approaches to glacier dynamics, and for a considerably smaller number of glaciers.

In this contribution, the length response of 91 glaciers from the data set of glacier length changes from the Swiss Glacier Monitoring Network (GLACIOLOGICAL REPORTS 2009) are analyzed. To this aim, a macroscopic glacier model is used which is formulated as a dynamical system in the variables length and volume (LÜTHI 2009). From the model results, parameters are obtained which are characteristic for these glaciers, the most important of which are the volume time scale as

well as constraints on the Little Ice Age equilibrium line history.

2 Data and methods

2.1 Length change data

The data set of glacier length changes from the Swiss Glacier Monitoring Network is used in this study (GLACIOLOGICAL REPORTS 2009). This publicly available data set contains 120 glacier length change records with yearly measurements. For 27 glaciers there are time series of more than 100 years, and 3 glaciers have been measured for more than 120 years (Fig. 1). In this study, the length changes for 91 of these glaciers are analyzed, which have a homogeneous data set covering at least 35 years.

2.2 LV-model

A macroscopic representation of glacier response to climate is used, formulated as a two-variable dynamical system in the variables «length» L and «volume» V (LÜTHI 2009). The dynamical system reproduces on a macroscopic scale the essential influence of mass balance and ice dynamics on glacier geometry, as represented with the variables L and V . Figure 2 illustrates the building blocks of the LV-model: two reservoirs of volumes V_A and V_B which are linked by a flux element located at horizontal coordinate G . The ice flux through a vertical section at the equilibrium line is determined by ice thickness and surface slope according to the shallow-ice approximation (HUTTER 1983). Local mass balance rate is parametrized as a linear function of elevation. From these assumptions, a system of two ordinary differential equations (ODE) can be derived (LÜTHI 2009, Eqs. 40)

$$\frac{1}{\gamma} \frac{dV}{dt} = V + ZL - \frac{m_b}{2} L^2 \quad (1a)$$

$$\tau_a \frac{dL}{dt} = \left(\frac{V}{a} \right)^{\frac{1}{\mu}} - L, \quad (1b)$$

where $\gamma = \frac{\partial b}{\partial z}$ is the vertical gradient of mass balance rate (in units of meter ice thickness per year), $m_b = \tan \beta$ is bedrock slope, τ_a is the relaxation time constant for the length adjustment, and parameters a and $\mu = 7/5$ describe the volume-length scaling relation. The scaling parameter a depends explicitly on γ and β (LÜTHI 2009, Eq. 21). The dynamical system (Eq. 1) contains an external forcing term in $Z(t) = z_0 - z_{ELA}(t)$, where z_0

is the highest point of the bedrock (Fig. 2), and $z_{\text{ELA}}(t)$ is the time dependent equilibrium line altitude (ELA). In vicinity of a steady state, the LV-model is equivalent to a linearly damped harmonic oscillator (HARRISON et al. 2003) which is slightly over-damped. The dynamical system (Eq. 1) was solved numerically with the PyDS-Tool toolkit (CLEWLEY et al. 2004).

2.3 Equilibrium line history

In the LV-model, local mass balance rate at the glacier surface is prescribed as a linear function of elevation $b(z) = \gamma(z - z_{\text{ELA}})$, with a constant vertical gradient γ of local mass balance rate. A changing climate is hence parametrized as a change in ELA, which appears as forcing in the Z term of the LV-model (Eq. 1a). To calculate glacier length changes, a history of ELAs was prescribed, which is based on a reconstructed record of temperature and precipitation of Europe since 1600 (CASTY et al. 2005). A spatial average of monthly data for 9 grid points centered in the Gotthard area was used.

To obtain ELA variations from temperature and precipitation, a bi-linear relation between temperature T , precipitation P and ELA was assumed of the form

$$z_{\text{ELA}}(t) = a + b\Delta T(t) + c \left(1 - \frac{\Delta P(t)}{P_{\text{ref}}}\right), \quad (2)$$

which is equivalent to a standard climate-ELA relation (OHMURA et al. 1992, Eq. 1) if the derivatives $\frac{\partial T}{\partial z}$ and $\frac{\partial P}{\partial T}$ are constant. The values of the constants were determined by fitting the parametrized ELA changes to reconstructed ELA variations for several Swiss glaciers (HUSS et al. 2008; HUSS 2009). The best agreement between the climate and ELA reconstructions was found for summer (JJA) temperature, and yearly average precipitation, with the constants $a = 2738$ m, $b = 101$ m K⁻¹, $c = 200$ m and $P_{\text{ref}} = 2000$ mm.

As will be shown below, the ELA reconstruction is not suitable to produce any of the big and rapid Little Ice Age glacier advances observed between 1650 and 1850. To achieve a match of measured length changes before 1910, the ELA had to be lowered by 100 to 200 m for certain periods within the time span 1650 to 1850.

3 Model results

The response of a glacier to climate forcing depends on its geometry, which in the LV-model is simply parametrized as bedrock slope β and vertical extent Z of the accumulation area. Driven by a history of ELA changes, glacier length changes were calculated with

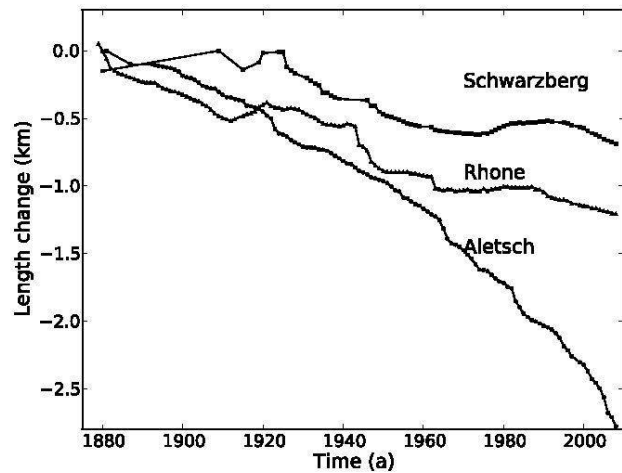


Fig. 1: Length changes of three glaciers of different length and mean slope and with a length change record exceeding 100 years: Grosser Aletschgletscher, Rhonegletscher, Schwarzberggletscher.

Längenänderungen von drei Gletschern mit unterschiedlicher Länge und mittlerer Neigung, deren Messdaten mehr als 100 Jahre abdecken: Grosser Aletschgletscher, Rhonegletscher, Schwarzberggletscher.

Variations de longueur de trois glaciers présentant des longueurs et des pentes différentes sur une période de plus de 100 ans: glacier d'Aletsch, glacier du Rhône et Schwarzberggletscher.

the LV-model in the following manner: The model glaciers were initialized to a steady state in the year 1600 for each set of parameters γ , β and Z . The model was driven with an ELA history calculated from temperature and precipitation from the climate reconstruction (Eq. 2). The ELA history used for the time span after 1880 is shown in Figure 3c, and the complete history in Figure 4b.

The influence of the geometry parameters on glacier length response is investigated in Figure 3. The ELA history shown in panel 3c was used to drive the LV-model (Eq. 1) for different values of β (Figure 3a) and Z (Figure 3b). It is immediately obvious that flat glaciers and glaciers with a small vertical extent show a very smooth response, and therefore have long response times. On the other hand, steep glaciers, and glaciers spanning a high elevation difference show a large and fast response to short-term fluctuations of the ELA.

The model results in Figure 3 look similar in character to the measured length change records from the data set (Figure 1). For a quantitative comparison, an optimization procedure was used to find a set of model parameters (γ , Z , β) which produces the best-match-

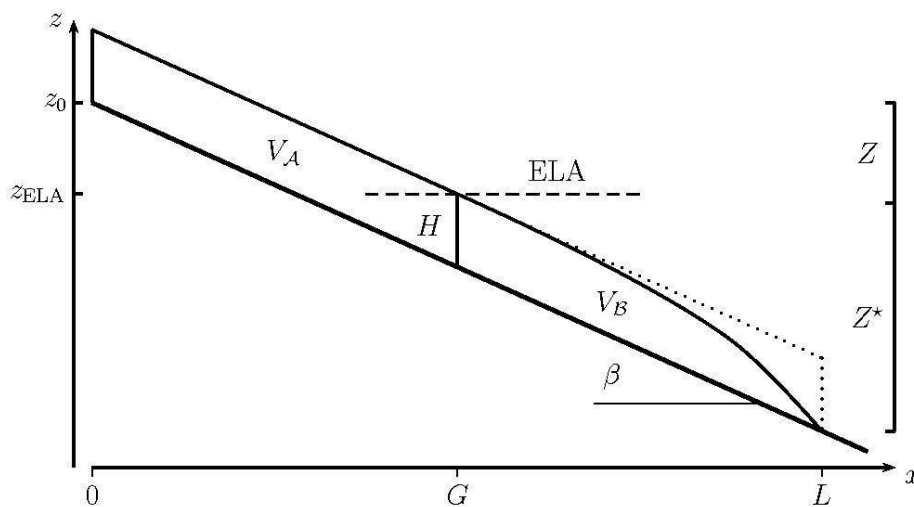


Fig. 2: A sketch of the LV-model geometry and relevant quantities
Skizze der Geometrie des LV-Modells und der geometrischen Grössen
Croquis de la géométrie du modèle LV et des tailles géométriques

ing length change history. With a set of parameters, the dynamical system was integrated forward in time for each of the ELA histories shown in Figure 4b as driving function (many more unsuccessful attempts are not shown). Each of the measured length change records was then compared to the responses of the model glaciers to find the closest match between real and model glaciers. The best overall agreement was obtained with $\gamma = 0.008 \text{ a}^{-1}$, which was adopted for all glaciers. The best fitting model glacier then yields the characteristic parameters Z and β , and from these the derived quantities «model glacier length» L and «volume time scale» τ_v can be determined.

The modeled glacier response is strongly influenced by the climate history assumed between 1650 and 1850, a climatic episode termed the «Little Ice Age» (LIA). For most glaciers, especially those with a long response time, it is impossible to obtain a reasonable fit between modeled and measured length changes if the model is forced with ELA variations according to the climate reconstruction of precipitation and temperature alone. Since mass balance also depends on variation of solar radiation (e.g. HUSS et al. 2009), and inspired by the reconstruction of the radiative forcing for the time span considered (e.g. CROWLEY 2000; STEINHILBER et al. 2009), the ELA was lowered during certain phases of the LIA. Taking Grosser Aletschgletscher as an example, Figure 4 shows the modeled response for three different LIA climates which differ only by a constant offset of the ELA during certain time spans. A reasonable agreement for the length change records of most glaciers could be obtained for an ELA low-

ered by 100 m between 1680 and 1720, and by 150 m between 1800 and 1850 (solid line in Figure 4b), which was adopted for the rest of this study.

Length change data for 91 glaciers of the Swiss Glacier Monitoring Network contain enough homogeneous data points to be fitted with modeled length changes. These best-fitting model glaciers capture the essential dynamics of a glacier terminus, and yield values for β , Z and the volume time scale τ_v . Figure 5 shows how well the individual glacier length records could be fitted with the LV-model. Table 1 lists characteristic quantities and model parameters for the glaciers. Also listed are inferred volume time scales which range from 5-20 years for very steep glaciers (e.g. Rosenlauri, Orny, Trient), 130-140 years for Grosser Aletschgletscher, and up to 160-180 years for several smaller glaciers. The increasingly large uncertainties of determined volume time scale for longer-timescale glaciers is due to the relatively short sampling interval of glacier response, as compared to the volume time scale.

The method works surprisingly well even for glaciers that would appear as problematic: heavily debris-covered glacier tongues (e.g. Unteraar, Zmutt; whereas Mont Durand cannot be fitted), glaciers that went through a strong topographic break during the sampling interval (e.g. Blüemlisalp, Eiger, Palü, Rhone, Tiatscha, Turtmann; whereas Mont Fort cannot be fitted), and glaciers that were affected by hydraulic dams (Unteraar, Oberaar, Gries) and natural lakes (Roseg, Gauli, Trift), where formation of a proglacial lake lead to temporarily fast retreat.

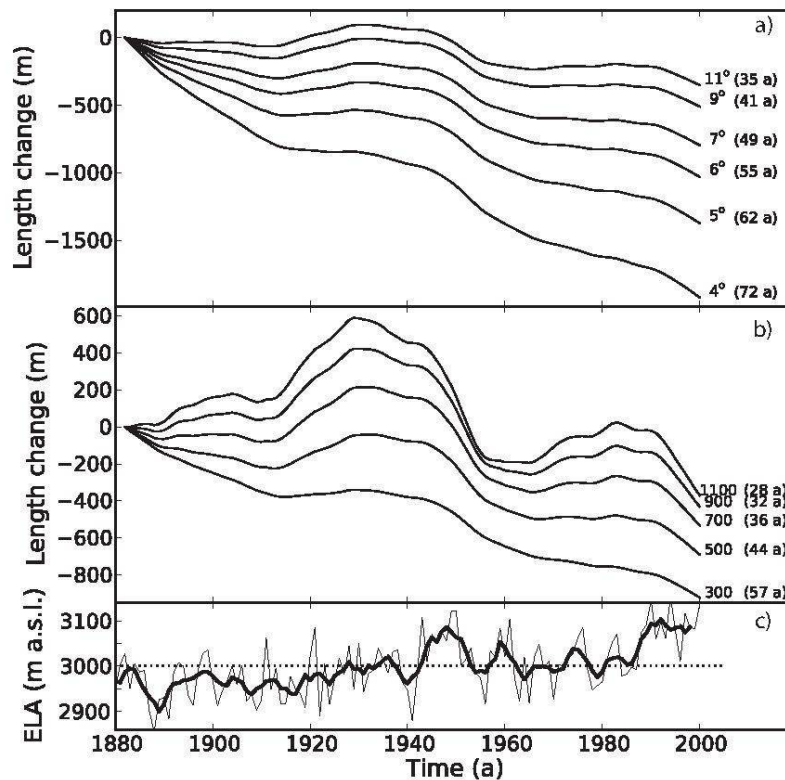


Fig. 3: Modeled length changes for glaciers of (a) different bedrock slopes β (for $Z = 400$ m) and (b) different vertical extents Z of the accumulation area (for $\beta = 7^\circ$). Values of β and Z are indicated next to curves, the volume time scale τ_v is given in parentheses. (c) The variation of equilibrium line altitude is shown as a thin line, and smoothed with a 5 years running average (wide line).

Modellierte Längenänderungen von Gletschern für (a) verschiedene Bettneigungen β (für $Z = 400$ m) und (b) für verschiedene vertikale Ausdehnungen des Akkumulationsgebietes Z (für $\beta = 7^\circ$). Werte von β oder Z sowie die Volumenzeitskala τ_v (in Klammern) sind neben den Kurven angegeben. (c) Die Variation der Gleichgewichtslinie ist als dünne, das 5-Jahres-Mittel als dicke Linie dargestellt.

Modélisation des changements de longueur des glaciers présentant (a) différentes pentes du soubassement rocheux β (pour $Z = 400$ m) et (b) différentes extensions verticales de la zone d'accumulation (pour $\beta = 7^\circ$). Les valeurs de β et de Z sont indiquées à côté des courbes, l'échelle temporelle τ_v est indiquée entre parenthèses. (c) La variation de l'altitude de la ligne d'équilibre est indiquée par une ligne fine tandis qu'une ligne épaisse indique des valeurs lissées avec une moyenne mobile de 5 ans.

4 Discussion

One cannot expect a perfect fit between modeled and measured length changes for several reasons. The assumed model geometry with an uniformly inclined bedrock is too simple to reproduce glacier length changes if they occur in a terrain with strong topographic changes, such as steps or changing valley widths in the terminus area. It is, however, astonishing that for most glaciers a simple model glacier can be found which has a similar length change response. The determined geometrical parameters β and Z (Table 1) are often surprisingly close to the real geometry, where β should be interpreted as mean slope of the ablation

area. The accumulation area is poorly represented in the LV-model since the usual flow convergence from a wide accumulation area, and the often constant accumulation rate at higher elevations, are neglected. Nevertheless, the essential features of the LV-model, namely the total mass flux from the accumulation area to the ablation area, and the constant mass balance gradient in an ablation area of constant width, seem like realistic approximations.

4.1 Volume time scale

How fast and to what extent a glacier reacts to changes in climate is largely determined by a single parameter, the volume time scale τ_v (HARRISON et al. 2001; JÓHAN-

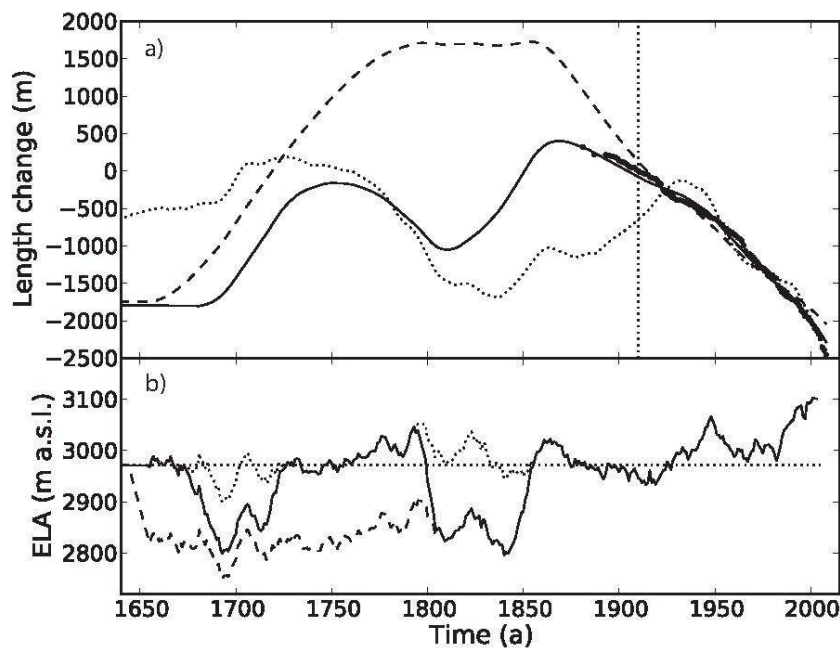


Fig. 4: (a) Length changes of a model glacier that fits the measured length changes of Grosser Aletschgletscher (dots). Dotted line corresponds to a climate reconstruction alone, dashed and solid lines indicate altered ELA histories. (b) The three climate scenarios, plotted as 11-year smoothed ELA variations, which were used to drive the LV-model.

(a) *Längenänderungen von Modellgletschern, die die gemessenen Längenänderungen des Grossen Aletschgletschers reproduzieren (Punkte). Die gepunktete Linie ist das Resultat, das auf der Klimarekonstruktion basiert, die durchbrochene und die durchgezogene Linie wurden mit veränderten Klimageschichten berechnet.* (b) *Die drei Klimageschichten, dargestellt als 11-Jahres-Mittel der Gleichgewichtslinie, welche als Antrieb für das LV-Modell gebraucht wurden.*

Variations de longueur d'un glacier modélisé correspondant aux variations enregistrées sur le glacier d'Aletsch (points). Les lignes en pointillés sont basées sur une reconstruction climatique unique, tandis que les lignes discontinues et continues indiquent des antécédents climatiques de la ligne d'équilibre (ELA) altérés. (b) *Les trois scénarios climatiques utilisés dans le modèle LV sont montrés ici avec un lissage de 11 ans de la variation d'altitude de la ligne d'équilibre (ELA).*

NESSON et al. 1989;). The volume time scale depends on a combination of geometric parameters, and is inversely proportional to the mass balance gradient γ (HARRISON et al. 2003; LÜTHI 2009)

$$\tau_v := - \left(\gamma + \frac{b_L}{H_e} \right)^{-1} = \frac{H_e}{(-b_L) - \gamma H_e} . \quad (3)$$

The volume time scale depends on the balance rate at the terminus $b_L = \gamma(z_0 - m_b L - z_{ELA}) = \gamma(Z - m_b L)$, and on the effective ice thickness $H_e = (dL/dV)^{-1}$ which is the slope of the length-volume relationship of steady state glaciers.

Volume time scales for steady state glaciers are shown as function of β and Z in Figure 6 for a mass balance gradient $\gamma = 0.008 \text{ a}^{-1}$, which is typical for Alpine glaciers. The figure shows that long volume time scales

should be expected for flat glaciers with little elevation difference. Short volume time scales, and therefore rapid reaction to climate change, are expected for steep glaciers and high elevation difference. Also indicated in Figure 6 are the names of the best-fitting model glaciers, plotted at the location of the model parameters.

It is noteworthy, that not only long glaciers (Grosser Aletschgletscher, Gorner, Otemma) have a long volume time scale, but also several smaller glaciers (e.g. Paradies, Roseg, Cheillon). The theory used to derive the LV-model explains that the volume time scale depends only on the «activity index» ζ like $\tau_v^{-1} = \gamma(\zeta - 1)$ (LÜTHI 2009). This parameter, defined by

$$\zeta := \frac{Z^*}{H_e} = \frac{m_b L - Z}{\mu f H} > 0, \quad (4)$$

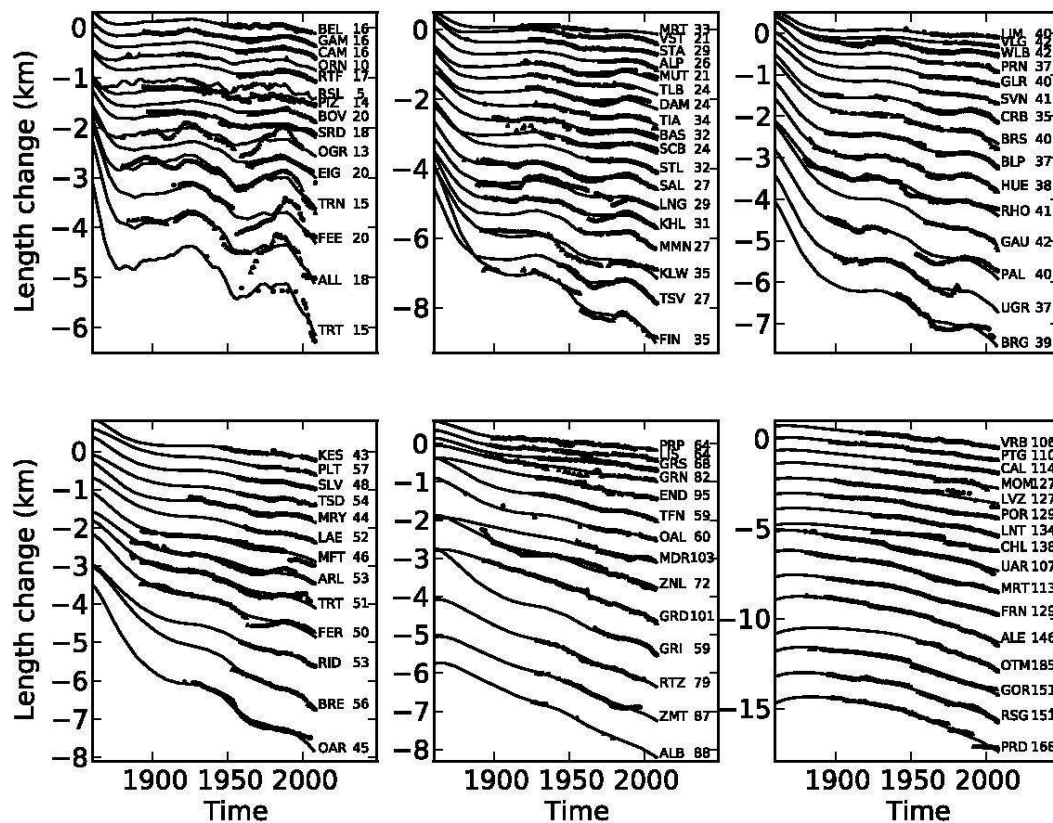


Fig. 5: Modeled length changes under the same climate are shown for 91 glaciers with solid lines (vertically shifted for clarity). Measured length changes are indicated with dots. At the end of each line, the 3 letter abbreviation of the glacier name (cf. Table 1) and the volume time scale are given.

Modellierte Längenänderungen für 91 Gletscher wurden mit der gleichen Klimageschichte als Antrieb berechnet (die Kurven sind der Übersichtlichkeit halber vertikal verschoben). Gemessene Längen sind mit Punkten dargestellt. Am Ende jeder Linie sind ein Kürzel des Gletschernamens (Tabelle 1) sowie die Volumenzeitskala angegeben.

Les lignes indiquent les variations de longueur modélisées pour 91 glaciers sur la base d'un climat identique (rendues verticales pour plus de clarté). Les variations de longueur mesurées sont indiquées par des points. A la fin de chaque ligne figurent les abréviations des noms des glaciers (voir Tableau 1) ainsi que l'échelle de temps.

only depends on geometric quantities, and parameters from the scaling relation (μ) and self-similarity (f), and can be visualized as the vertical extent of the ablation area Z^* scaled by the effective ice thickness $H_e \sim 1.23 H$ (shown in Fig. 2).

4.2 Climate

The glacier length variations during the last 150 years of all 91 investigated glaciers can be explained with a single history of ELA variation, and a constant mass balance gradient of $\gamma = 0.008 \text{ a}^{-1}$. The similar variation of the ELA throughout the whole Swiss Alps, despite large differences in local climate, is attributable to the strong dependence of ELA on temperature. Air temperature anomalies are well correlated in the Alpine area (e.g. CASTY et al. 2005).

The measured glacier length changes could only be reproduced with the LV-model if the ELA history (calculated from a reconstructed temperature and precipitation history) was considerably altered during certain periods of the LIA. The marked advance of most glaciers between 1830 and 1850 cannot be reproduced without such an ELA alteration.

The necessity to alter the ELA-history can have several reasons:

- Reconstructed air temperature and precipitation rely mainly on data from low elevation stations, especially before the 20th century, which might result in a misrepresentation of the reconstructed climate at high elevations.
- The time spans of altered ELA correspond to phases

Name	Short	Length	Time span	#meas.	β	Z	ζ	τ_v
Rosenloui	RSL	5.2	1923 - 1988	27	41.5	1750	27.37	5
Orny	ORN	2.9	1881 - 1989	22	41.3	483	13.27	10
Ob. Grindelwald	OGR	6.7	1878 - 2000	98	25.2	741	10.67	12
Pizol	PIZ	0.6	1892 - 2008	95	33.3	416	9.97	13
Trient	TRN	4.9	1878 - 2008	128	13.8	1450	9.61	14
Trift	TRT	5.8	1860 - 2008	17	8.2	2700	9.24	15
Bella Tola	BEL	0.6	1944 - 2005	57	40.0	250	9.06	15
Cambrena	CAM	1.9	1955 - 2008	46	39.0	250	8.84	15
Gamchi	GAM	2.8	1893 - 2008	101	39.0	250	8.84	15
Rotfirm	RTF	2.1	1955 - 2008	50	36.5	250	8.31	17
Sardona	SRD	0.7	1894 - 2008	94	24.8	450	8.13	17
Allalin	ALL	6.5	1880 - 2008	114	9.0	1733	7.83	18
Boveyre	BOV	2.6	1963 - 2008	37	28.8	300	7.47	19
Fee	FEE	5.0	1913 - 2008	86	11.0	1150	7.31	19
Eiger	EIG	2.6	1962 - 2008	43	17.0	625	7.29	19
Verstankla	VST	2.1	1925 - 2008	71	27.8	275	6.95	21
Mutt	MUT	1.0	1917 - 2008	70	24.0	341	6.93	21
Tälliboden	TLB	0.8	1921 - 1992	56	19.2	383	6.27	23
Schwarzberg	SCB	3.8	1879 - 2008	77	17.8	425	6.23	23
Damma	DAM	2.4	1920 - 2003	80	18.8	375	6.09	24
Alpetli	ALP	6.8	1969 - 2008	39	21.8	275	5.82	25
Saleina	SAL	6.5	1877 - 2008	116	12.9	558	5.74	26
Mont Miné	MMN	8.3	1955 - 2007	44	9.2	866	5.67	26
Tschierva	TSV	4.8	1933 - 2008	63	7.7	1041	5.52	27
Sankt Anna	STA	0.8	1866 - 2008	75	21.5	225	5.27	29
Lang	LNG	6.9	1887 - 2008	109	12.2	500	5.26	29
Basodino	BAS	1.5	1898 - 2008	84	15.8	316	5.05	30
Kehlen	KHL	2.6	1892 - 2008	107	11.2	500	5.01	31
Steinlimmi	STL	2.8	1960 - 2008	47	12.0	425	4.85	32
Martinets	MRT	1.9	1918 - 1975	37	32.0	100	4.83	32
Kaltwasser	KLW	1.6	1890 - 2008	102	7.8	700	4.65	34
Findelen	FIN	7.8	1892 - 2008	79	4.8	1350	4.65	34
Tiatscha	TIA	2.0	1893 - 2008	71	15.2	275	4.63	34
Blümlisalp	BLP	2.7	1892 - 2008	101	11.7	366	4.47	36
Corbassière	CRB	10.2	1888 - 2008	71	14.8	258	4.44	36
Paradisino	PRN	1.1	1954 - 2008	41	19.2	175	4.40	36
Unt. Grindelwald	UGR	8.3	1899 - 1983	82	7.3	633	4.32	37
Hüfi	HUE	7.1	1881 - 2008	116	10.7	375	4.29	38
Brunegg	BRG	4.6	1933 - 2005	65	6.8	675	4.23	38
Bresciana	BRS	1.1	1895 - 2008	81	11.8	308	4.19	39
Palü	PAL	3.8	1893 - 2008	76	7.5	550	4.12	40
Glärnisch	GLR	2.5	1956 - 2008	48	17.2	175	4.12	40
Rhone	RHO	8.0	1878 - 2008	128	9.9	375	4.11	40
Limmern	LIM	3.1	1944 - 2008	44	29.8	75	4.07	40
Wallenbur	WLB	1.9	1892 - 2008	101	20.8	125	4.00	41
Valleggia	VLG	0.9	1970 - 2008	29	28.5	75	3.95	42
Sesvenna	SVN	1.2	1955 - 2008	49	15.0	191	3.95	42
Gauli	GAU	6.5	1957 - 2008	47	7.8	458	3.92	42
Moiry	MRY	5.3	1924 - 2005	79	13.9	208	3.92	42
Kessjen	KES	0.9	1945 - 2008	50	19.8	125	3.89	43
Oberaar	OAR	5.0	1920 - 2005	76	5.0	750	3.75	45
Mont Fort	MFT	2.1	1891 - 2007	103	12.2	216	3.70	46
Silvretta	SLV	3.3	1956 - 2008	49	15.2	150	3.62	47
Ferpecle	FER	6.6	1890 - 2007	111	7.8	350	3.51	49
Turtmann	TRT	5.8	1884 - 2005	114	9.0	275	3.46	50

Name	Short	Length	Time span	#meas.	β	Z	ζ	τ_v
Ried	RID	6.3	1957 - 2008	47	7.5	325	3.36	52
Arolla	ARL	4.8	1885 - 2007	114	10.7	200	3.35	50 - 56
Tseudet	TSD	3.0	1956 - 2008	46	14.8	125	3.33	53
Lämmern	LAE	2.6	1960 - 2008	48	11.9	166	3.31	54
Breney	BRE	6.0	1952 - 2008	52	5.2	475	3.24	55
Tiefen	TFN	3.0	1926 - 2008	78	11.3	166	3.24	53 - 59
Plattalva	PLT	1.4	1968 - 2008	32	16.0	100	3.20	56
Gries	GRI	5.7	1966 - 2008	42	6.8	300	3.11	56 - 61
Lischana	LIS	0.9	1894 - 2008	84	22.2	50	2.97	63
Prapio	PRP	0.8	1897 - 2005	84	22.2	50	2.97	63
Oberaletsch	OAL	9.1	1869 - 2007	40	10.9	133	2.95	60 - 66
Griess	GRS	1.6	1928 - 2008	71	20.2	50	2.84	68
Zinal	ZNL	7.5	1890 - 2007	114	8.5	150	2.74	66 - 78
Rätzli	RTZ	5.2	1924 - 2000	63	6.6	175	2.59	72 - 84
Griessen	GRN	1.2	1893 - 2007	75	15.2	50	2.52	82
Zmutt	ZMT	6.7	1927 - 1997	54	6.2	150	2.44	80 - 94
Albigna	ALB	3.7	1905 - 1979	13	5.4	175	2.41	82 - 96
Lavaz	LVZ	2.1	1899 - 2008	80	7.9	108	2.43	66 - 126
Endarrey	END	2.1	1879 - 2008	66	12.0	50	2.31	95
Grand Desert	GRD	2.2	1891 - 2008	108	6.5	108	2.28	89 - 103
Vorab	VRB	2.0	1916 - 2008	69	10.2	58	2.27	87 - 105
Mont Durand	MDR	5.9	1954 - 2007	49	10.5	50	2.21	103
Unteraar	UAR	12.9	1875 - 2005	114	5.0	133	2.20	96 - 109
Moming	MOM	3.6	1926 - 2001	68	7.4	83	2.23	82 - 126
Calderas	CAL	1.8	1952 - 2008	52	8.8	58	2.17	96 - 113
Punteglias	PTG	1.4	1894 - 2008	100	9.2	50	2.13	110
Morteratsch	MRT	7.0	1877 - 2008	122	4.5	116	2.08	109 - 125
Forno	FRN	6.2	1894 - 2008	97	4.2	108	2.02	112 - 129
Porchabella	POR	2.4	1892 - 2008	100	6.8	50	1.97	129
Lenta	LNT	2.6	1924 - 2008	73	6.2	50	1.94	133
Grosser Aletsch	ALE	23.9	1869 - 2008	118	3.2	116	1.93	127 - 146
Cheillon	CHL	3.7	1823 - 2008	79	5.8	50	1.90	135 - 141
Gorner	GOR	13.5	1881 - 2008	112	2.8	100	1.84	149
Roseg	RSG	4.9	1894 - 2008	100	2.7	91	1.80	150 - 167
Paradies	PRD	3.6	1872 - 2008	99	2.2	116	1.79	152 - 167
Otemma	OTM	8.7	1954 - 2008	48	2.3	66	1.72	156 - 185

Tab. 1: Volume time scales for 91 glaciers as inferred from the model results. Given are glacier name, 3 letter abbreviation, length in the year 1973 (in km; MAISCH 2001), time span and number of measurements used, the values of model parameters β , Z and ζ , and the volume time scale.

Volumenzeitkalen für 91 Gletscher, bestimmt aus den Modell-Resultaten. Angegeben sind: Gletschernaame, Kürzel, Länge im Jahr 1973 (in km; MAISCH 2001), Zeitspanne und Anzahl Messungen, Werte der Modellparameter β , Z und ζ sowie die Volumenzeitkala.

Echelles de temps pour 91 glaciers tel qu'estimé par le modèle. Sont indiqués le nom des glaciers, leur abréviation, leur longueur en 1973 (en km, voir MAISCH 2001), la période et le nombre de mesures effectuées, la valeur des paramètres β , Z and ζ du modèle ainsi que l'échelle temporelle.

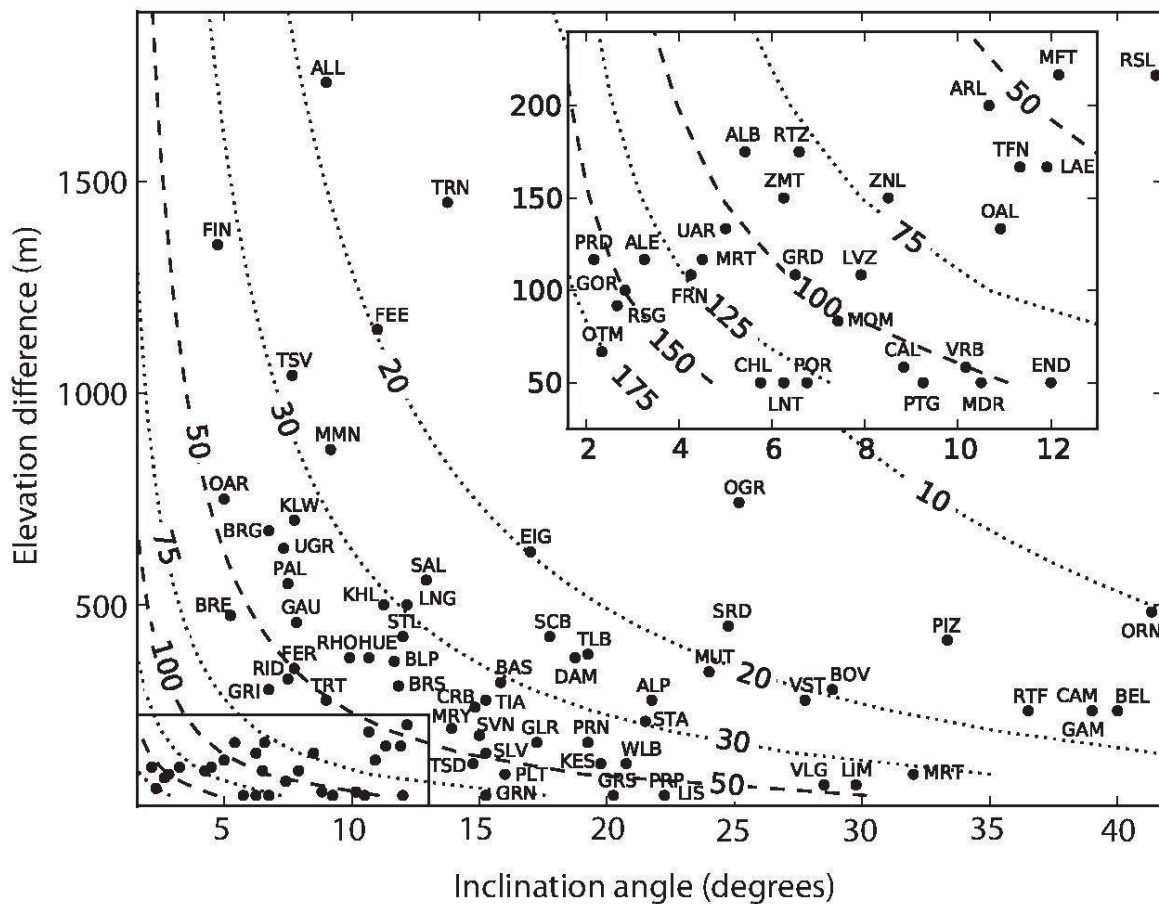


Fig. 6: Contours show volume time scale τ_v (in years) in dependence of bedrock inclination angle β and vertical extent of the accumulation area Z . Parameter values of the best-fitting models are indicated with a dot for each glacier (3 letter abbreviation, cf. Table 1). Inset shows the enlargement of the lower left corner.

*Konturen stellen die Volumenzeitskala τ_v (in Jahren) in Abhängigkeit von der Bettneigung β und der Vertikal-
ausdehnung Z des Akkumulationsgebietes dar. Die Parameterwerte für die Modellgletscher mit der besten Über-
einstimmung sind als Punkte dargestellt und mit dem Kürzel des Gletschernamens versehen (vgl. Tabelle 1). Die
kleine Graphik ist ein vergrößerter Ausschnitt des unteren linken Bereiches.*

*Les contours montrent l'échelle de temps τ_v (en années) selon l'angle d'inclinaison du soubassement rocheux β et
l'extension verticale de la zone d'accumulation Z . Les valeurs des modèles les plus adaptés sont indiquées avec
un point pour chaque glacier (pour les abréviations, voir Tableau 1). L'encart montre une vue agrandie du coin
inférieur gauche.*

of reduced incoming solar radiation caused by changes in total solar irradiance (STEINHILBER et al. 2009) and/or high volcanic dust concentrations in the atmosphere (e.g. CROWLEY 2000).

- Mass balance gradients are not constant in time. A step-wise change in mass balance gradient leads to a fast glacier tongue retreat due to enhanced melting, and a long-term advance when the increased mass gain has been transported from the accumulation area to the terminus. Since mass balance gradients change independent of ELA, it is very difficult to assess their relative importance.

The approach used above of lowering the ELA does not discern between the above possibilities, but corroborates the necessity of ELA changes during the LIA. The problem of explaining the LIA glacier mass gain with mass balance reconstructions based on temperature and precipitation has been discussed before (NESJE & DAHL 2003; VINCENT et al. 2005). It is not clear at present, whether such a disagreement can be explained by an increased winter precipitation within the inner Alpine region (as advocated by VINCENT et al. 2005), or due to other changes in climate parameters, such as an altered radiation budget.

5 Conclusions

The glacier length change record of 91 glaciers from the Swiss Glacier Monitoring Network was analyzed with help of a macroscopic glacier model. By fitting modeled length changes to measurements, the parameters of the best-fitting model could be determined for each glacier. The measured length changes of all 91 glaciers can be explained with a single history of ELA variations. From the model parameters, the volume time scale can be determined, which ranges from 5 to 170 years, depending on inclination and vertical extent of the glaciers.

The glacier length change records cannot be interpreted by using an equilibrium line history based on reconstructed temperature and precipitation alone. During certain phases of the Little Ice Age (1650-1850) the ELA must have been lower by 100 to 200 m, probably caused by increased winter precipitation, or by other changes in climate parameters such as reduced global radiation.

The proposed analysis of glacier length changes can be applied to other mountain ranges with similar data sets, and to longer glacier length change histories, and might thus be used to constrain the regional Alpine climate during the Little Ice Age.

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Abstract: Analysis of Alpine glacier length change records with a macroscopic glacier model

The length change record of 91 glaciers in the Swiss Alps was analyzed with a novel macroscopic glacier model (LV-model). Based on a history of equilibrium line variations, synthetic length change data were calculated. From the LV-models matching best the measured length changes, characteristic parameters were obtained. The volume time scale thus determined ranges from 5 to 170 years for glaciers of different slope and length. The analysis shows that the observed glacier length changes cannot be reproduced with an equilibrium line variation based on temperature and precipitation alone. The equilibrium line has to be lowered by 100 to 200 meters during several phases of the Little Ice Age (in the time span 1650 to 1850) to obtain observed glacier responses. Such an effect might be attributable to either higher winter precipitation in the Alps, or to radiation forcing.

Keywords: glacier, climate, Alps, length change, dynamical system

Zusammenfassung: Analyse der Längenänderungen von Alpengletschern mit einem makroskopischen Gletschermodell

Die Längenänderungen von 91 Gletschern der Schweizer Alpen wurden mit einem neuartigen makroskopischen Gletschermodell (LV-Modell) analysiert. Ausgehend von einer Geschichte von Höhenänderungen der Gleichgewichtslinie wurden Längenänderungen berechnet. Das LV-Modell mit der besten Übereinstimmung mit gemessenen Längenänderungen ermöglicht die Bestimmung charakteristischer Grössen, aus denen die Volumenzeitskala bestimmt werden kann. Je nach Neigung und Länge variiert diese zwischen

fünf und 170 Jahren. Die Methode zeigt, dass sich die gemessenen Längenänderungen nicht reproduzieren lassen, wenn die Änderungen der Gleichgewichtslinie nur von den rekonstruierten Temperaturen und Niederschlägen abhängen. Die Gleichgewichtslinie muss während verschiedener Phasen der «Kleinen Eiszeit» (1650 bis 1850) um 100 bis 200 Meter tiefer gelegen haben, um die beobachtete Reaktion der Gletscher zu erklären. Ein solcher Effekt könnte entweder auf höhere Winterniederschläge in den Alpen oder auf eine geringere Strahlung zurückzuführen sein.

Schlüsselwörter: Gletscher, Klima, Alpen, Längenänderung, dynamische Systeme

Résumé: Analyse des variations de longueur des glaciers suisses: un modèle glaciaire macroscopique

Nous avons analysé les mesures des variations de longueur de 91 glaciers des Alpes suisses au moyen d'un nouveau modèle glaciaire macroscopique (modèle LV). Nous avons calculé des données synthétiques de variations de longueur de glaciers sur la base d'une série se rapportant aux altitudes de la ligne d'équilibre pour les années passées. En adaptant au mieux le modèle LV aux données des variations de longueur, nous avons obtenu des paramètres propres à chaque glacier. L'échelle de temps obtenue pour les différents glaciers varie entre 5 et 170 années suivant la pente et la longueur des glaciers. Notre analyse a montré que les variations de longueur observées ne peuvent être expliquées par des fluctuations de la ligne d'équilibre basées sur les températures et les précipitations. L'altitude de la ligne d'équilibre a dû être abaissée de 100 à 200 mètres durant certaines périodes du Petit Âge glaciaire (entre 1650 et 1850) pour obtenir les variations observées sur les glaciers. Cet effet peut être attribué soit à des précipitations plus élevées dans les Alpes, soit à une radiation solaire réduite.

Mots-clés: glacier, climat, Alpes, changement de longueur, système dynamique

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